

# Gravitational Recoil and Astrophysical impact

U. Sperhake

DAMTP, University of Cambridge



3<sup>rd</sup> Sant Cugat Forum on Astrophysics  
25<sup>th</sup> April 2014

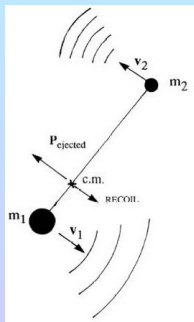
# Overview

- Introduction and motivation
- Calculation of the recoil
- Suppression of superkicks
- Unknown
- Unknown
- Conclusions

# 1. Introduction, motivation

# Gravitational recoil

- **Recoil** = move abruptly backward as a reaction on firing a bullet, shell, or other missile



- **Anisotropic GW emission**  
⇒ Gravitational recoil
- Here: **Black-hole binary kicks**  
Also relevant for **supernovae**

# Gravitational recoil

- **Anisotropic GW emission**  $\Rightarrow$  recoil of remnant BH

Bonnor & Rotenberg 1961, Peres 1962, Bekenstein 1973

- **Escape velocities:**

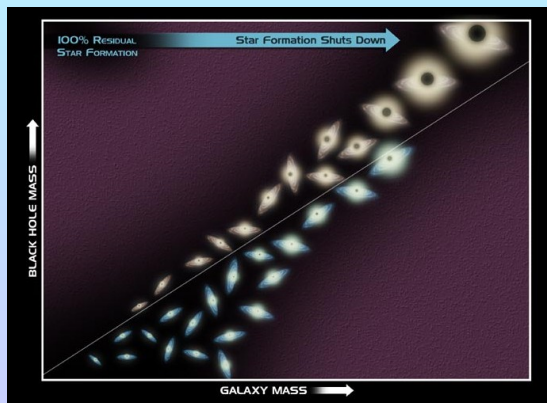
Globular clusters	30 km/s
dSph	20 – 100 km/s
dE	100 – 300 km/s
Giant galaxies	$\sim$ 1000 km/s

- **Ejection / displacement of BH**



# Motivation: Galaxies harbor BHs

- Galaxies ubiquitously harbor BHs
- BH properties correlated with bulge properties  
e. g. J. Magorrian *et al.*, AJ 115, 2285 (1998)



# Motivation: Formation history of SMBHs

- Most widely accepted scenario for galaxy formation: hierarchical growth; “bottom-up”
- Galaxies undergo frequent mergers, especially elliptic ones

large kicks

⇒ ejection of BHs

⇒ BH assembly possible?

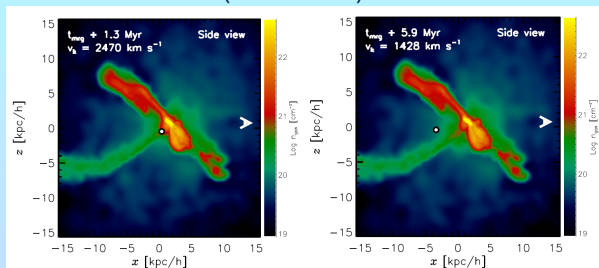
Higher accretion needed?

E.g. Merrit et al 2004



# Motivation: Ejection of SMBHs

recoil AGN (Blecha et al) double AGN



- Doppler shifts of BLR vs. NLR:  $2650 \text{ km/s}$ ; Komossa *et al.* 2008
- Galaxy CID-42: Double AGN or recoiling AGN? Blecha *et al.* 2012
- BH wandering from NGC 1275 to NGC 1277? Shields & Bonning 2013
- Review: Komossa 2012



# Motivation: BH ejection, BH populations

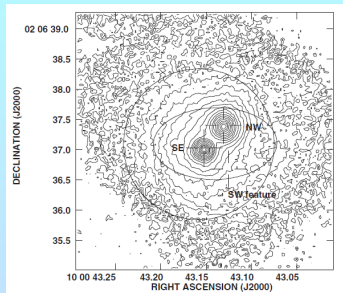
- Hierarchical growth  $\Rightarrow$  BH mergers
- Most massive dark matter halos at  $z \geq 11$ :  
BHs not retained if  $v_{\text{kick}} \gtrsim 150 \text{ km/s}$   
 $\Rightarrow$  Even modest kicks suppress SMHB growth from seed BHs  
 $\Rightarrow$   $>$ Eddington accretion needed to assemble SMBHs by  $z \approx 6$ ?  
e.g. Merrit et al 2004, Micic et al 2006
- Ejection affects BH populations  
e.g. Holley-Bockelmann et al 2008, Miller & Lauburg 2009
- BH depleted globular clusters? e.g. Mandel et al 2008
- Kicks impact event rates for GW observatories

# Motivation: Displacement of SMBHs, Elm signature

- Quasars kinematically or spatially offset from host galaxy

- E.g. COSMOSJ1000+0206:  
2 optical nuclei, 2 kpc apart

Wrobel 2014



- Moving BH  $\Rightarrow$  tidal disruption of star  $\Rightarrow$  X ray flares

Komossa & Bade 1999, Bloom et al 2011, Komossa & Merrit 2008a,

- BHs oscillating on scale of accretion torus  $\Rightarrow$  repeated flares

Komossa & Merrit 2008b

- BH velocity relative to accreted gas Lora-Calvijo & Guzman 2013

## 2. Calculation of kicks

# Influential work pre NR

- Non-spinning, equal-mass BH binaries
  - ⇒ no kick by **symmetry**
  - ⇒ Symmetry breaking through **mass ratio** or **spins**
- Quasi-Newtonian calculation for unequal masses (no spins)

Fitchett 1983

$$v_{\text{kick}} = A\eta^2\sqrt{1 - 4\eta(1 + B\eta)}, \quad \eta = \frac{q}{(1+q)^2}, \quad q = \frac{m_2}{m_1}$$

But: **Amplitude** unclear.

- PN calculations including spin-orbit coupling

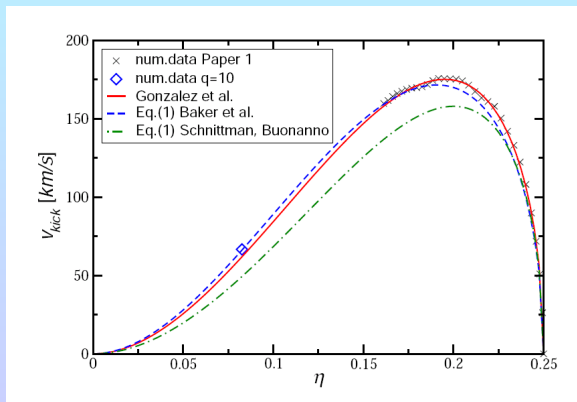
Kidder 1995

$$\frac{d\mathbf{P}}{dt} = \frac{d\mathbf{P}_F}{dt} + \frac{d\mathbf{P}_{SO}}{dt}, \quad \frac{d\mathbf{P}_F}{dt} = \text{Fitchett}, \quad \frac{d\mathbf{P}_{SO}}{dt} = \text{spin-orbit contr.}$$

# Kicks from non-spinning BHs

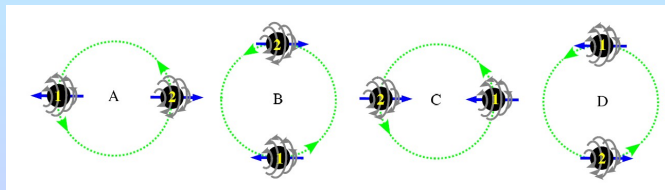
- NR simulations for BH binaries with  $q \in [0.1, 1]$   
 $\Rightarrow$  Max. kick:  $\sim 175$  km/s for  $q = 0.36$

González et al 2007a, 2009



# Kicks from spinning BHs

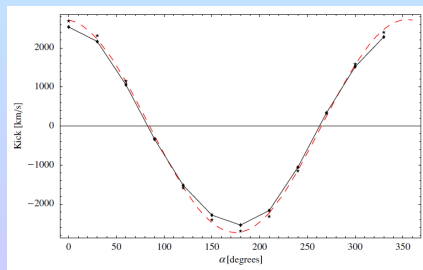
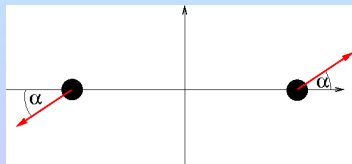
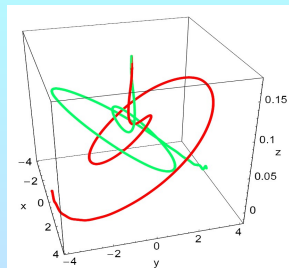
- Spins  $\mathbf{S} \parallel \mathbf{L}$  but  $\mathbf{S}_1 \neq \mathbf{S}_2$   
 $\Rightarrow$  kicks up to  $v_{\text{kick}} \lesssim 500 \text{ km/s}$   
Herrmann *et al* 2007, Koppitz *et al* 2007
- Kidder 1995, Campanelli *et al* 2007a: maximum kick expected for



“Superkicks”:  $\mathbf{S}_1 = -\mathbf{S}_2$  in orbital plane

# Superkicks

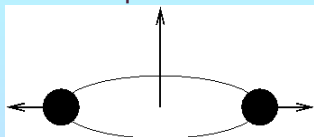
- Measured:  $v_{\text{kick}} \approx 2500$  km/s  
Extrapolated maximum:  $\sim 4000$  km/s  
González et al 2007b, Campanelli et al 2007b
- Sinusoidal dependency on spin orientation  $\alpha$



# Even larger kicks: superkick and hang-up

Lousto & Zlochower, PRL **107** 231102

Superkicks

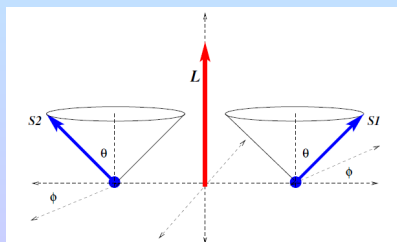


Hangup



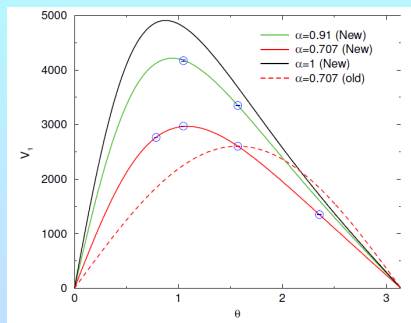
- Moderate GW generation
- Large kicks

- Strong GW generation
- No kicks





# Superkicks and orbital hang-up



- Maximum kick about 25 % larger:  $v_{max} \approx 5000$  km/s
- Distribution asymmetric in  $\theta$ ;  $v_{max}$  for partial alignment
- Higher order corrections to hang-up kick  
 $\Rightarrow$  Further 10 % increase “Cross-kick”

Lousto & Zlochower 2013

# Fitting formulae for the kick

- Goal: Machine, in: BH parameters, out:  $v_{\text{kick}}$

- Campanelli 2007b

$$\vec{V}_{\text{kick}}(q, \vec{\alpha}_i) = v_m \mathbf{e}_1 + v_{\perp} [\cos \xi \mathbf{e}_1 + \sin \xi \mathbf{e}_2] + v_{\parallel} \mathbf{e}_{\parallel},$$

$$v_m = A \frac{q^2(1-q)}{(1+q)^5} \left[ 1 + B \frac{q}{(1+q)^2} \right],$$

$$v_{\perp} = H \frac{q^2}{(1+q)^5} \left( \alpha_2^{\parallel} - q \alpha_1^{\parallel} \right),$$

$$v_{\parallel} = K \cos(\Theta - \Theta_0) \frac{q^2}{(1+q)^5} |\vec{\alpha}_2^{\perp} - q \vec{\alpha}_1^{\perp}|$$

- $A = 1.2 \times 10^4$  km/s,  $B = -0.93$ ,  $H = 7.3 \times 10^3$  km/s,  $\xi \sim 145^\circ$

$$\vec{\alpha}_i = \mathbf{S}_i / m_i^2, \quad \Theta = \text{infall angle}$$

# Fitting formulae for the kick

## Extensions of the fitting formula

- Systematic spin expansion,  
exploit **symmetry** conditions to reduce terms Boyle, Kesden & Nissanke 2007, 2007a
- Calibration of higher-order spin terms,  
 $\sim 100$  NR simulations ( $q = 1$ ) Lousto & Zlochower 2013
- Ongoing work; more simulations required

# 3. Open questions

# Open problems with current kick predictions

- Mass ratio  $q$ 
  - Current calibration through  $q = 1$  runs
  - Predictions for  $q < 1$  **uncertain**; too large?
  - **Solution**: More runs
- BH parameters
  - Fitting formulae apply to parameters shortly before merger
  - Astrophysical BH parameters apply to large separations
  - What happens to the statistical spin distribution during inspiral?
- Almost all galaxies harbor BHs
  - Superkicks easily eject BHs from giant hosts
  - Why are BHs still there?

- Superkicks easily eject BHs from their host galaxies
- **But:** Almost all observed galaxies host BHs
- How probable are superkicks?
  - EOB study of  $q \in [0.1, 1]$ ,  $\alpha_j = 0.9$ 
    - $\Rightarrow \sim 3\%$  with  $v_{\text{kick}} > 500$  km/s,  $\sim 12\%$  with  $v_{\text{kick}} > 1000$  km/s
    - Schnittman & Buonanno 2007
  - Gas-rich mergers tend to align  $\mathbf{S}_{1,2}$  with  $\mathbf{L}$ 
    - $10$  ( $30$ ) $^\circ$  residual misalignment for cold (hot) gas
    - $\Rightarrow$  superkick suppression
    - Bogdanović et al 2010, Dotti et al 2009
  - PN inspiral of isotropic BH ensemble remains isotropic
    - Bogdanović et al 2010
    - But:** How about non-isotropic ensembles?

# 4. Spin orbit resonances

# Parameters of a black-hole binary

10 **intrinsic** parameters for quasi-circular orbits

- 2 masses  $m_1, m_2$
- 6 for two spins  $\mathbf{S}_1, \mathbf{S}_2$
- 2 for the direction of the orbital ang. mom.  $\hat{\mathbf{L}}$ .

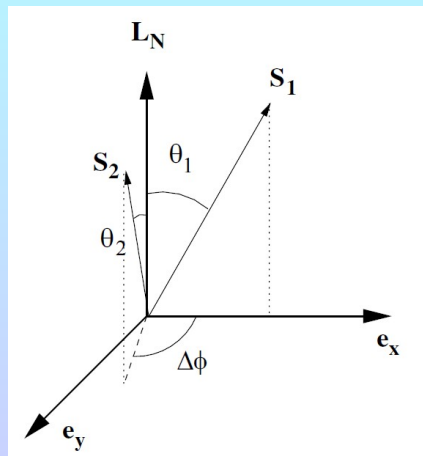
Elimination of parameters in PN inspiral

- 1 mass; **scale invariance**
- 2 for  $\hat{\mathbf{L}}$ ; **fix  $z$  axis**
- 2 spin magnitudes, 1 mass ratio  $q$ ; **conserved**
- 1 spin direction; **fix  $x$  axis**



# Evolution variables

⇒ Three variables:  $\theta_1, \theta_2, \Delta\phi$



# Evolution equations

$$\frac{d\mathbf{S}_1}{dt} = \boldsymbol{\Omega}_1 \times \mathbf{S}_1, \quad M\boldsymbol{\Omega}_1 = \eta v^5 \left( 2 + \frac{3q}{2} \right) \hat{\mathbf{L}} + \frac{v^6}{2M^2} \left[ \mathbf{S}_2 - 3 \left( \hat{\mathbf{L}} \cdot \mathbf{S}_2 \right) \hat{\mathbf{L}} - 3q \left( \hat{\mathbf{L}} \cdot \mathbf{S}_1 \right) \hat{\mathbf{L}} \right];$$

$$\frac{d\mathbf{S}_2}{dt} = \boldsymbol{\Omega}_2 \times \mathbf{S}_2, \quad M\boldsymbol{\Omega}_2 = \eta v^5 \left( 2 + \frac{3}{2q} \right) \hat{\mathbf{L}} + \frac{v^6}{2M^2} \left[ \mathbf{S}_1 - 3 \left( \hat{\mathbf{L}} \cdot \mathbf{S}_1 \right) \hat{\mathbf{L}} - \frac{3}{q} \left( \hat{\mathbf{L}} \cdot \mathbf{S}_2 \right) \hat{\mathbf{L}} \right];$$

$$\frac{d\hat{\mathbf{L}}}{dt} = -\frac{v}{\eta M^2} \frac{d}{dt} (\mathbf{S}_1 + \mathbf{S}_2);$$

$$\begin{aligned} \frac{dv}{dt} = & \frac{32}{5} \frac{\eta}{M} v^9 \left\{ 1 - v^2 \frac{743 + 924\eta}{336} + v^3 \left[ 4\pi - \sum_{i=1,2} \chi_i (\hat{\mathbf{S}}_i \cdot \hat{\mathbf{L}}) \left( \frac{113}{12} \frac{m_i^2}{M^2} + \frac{25}{4} \eta \right) \right] \right. \\ & + v^4 \left[ \frac{34103}{18144} + \frac{13661}{2016} \eta + \frac{59}{18} \eta^2 + \frac{\eta \chi_1 \chi_2}{48} \left( 721 (\hat{\mathbf{S}}_1 \cdot \hat{\mathbf{L}}) (\hat{\mathbf{S}}_2 \cdot \hat{\mathbf{L}}) - 247 (\hat{\mathbf{S}}_1 \cdot \hat{\mathbf{S}}_2) \right) \right. \\ & \left. \left. + \frac{1}{96} \sum_{i=1,2} \left( \frac{m_i \chi_i}{M} \right)^2 \left( 719 (\hat{\mathbf{S}}_i \cdot \hat{\mathbf{L}})^2 - 233 \right) \right] - v^5 \pi \frac{4159 + 15876\eta}{672} \right. \\ & + v^6 \left[ \frac{16447322263}{139708800} + \frac{16}{3} \pi^2 - \frac{1712}{105} (\gamma_E + \ln 4v) + \left( \frac{451}{48} \pi^2 - \frac{56198689}{217728} \right) \eta + \frac{541}{896} \eta^2 - \frac{5605}{2592} \eta^3 \right] \\ & \left. + v^7 \pi \left[ -\frac{4415}{4032} + \frac{358675}{6048} \eta + \frac{91495}{1512} \eta^2 \right] + O(v^8) \right\}; \end{aligned}$$

- 2.5 PN: precessional motion about  $\hat{\mathbf{L}}$
- 3 PN: spin-orbit coupling

# Schnittman's resonances

Schnittman '04

For a given separation  $r$  of the binary, resonances are

- $\mathbf{S}_1$ ,  $\mathbf{S}_2$ ,  $\hat{\mathbf{L}}_N$  lie in a plane  $\Rightarrow \Delta\phi = 0^\circ, \pm 180^\circ$
- Resonance condition:  $\ddot{\theta}_{12} = \dot{\theta}_{12} = 0$  Apostolatos '96, Schnittman '04
- $\Delta\phi = 0^\circ$  resonances: **always**  $\theta_1 < \theta_2$   
 $\Delta\phi = \pm 180^\circ$  resonances: **always**  $\theta_1 > \theta_2$
- The resonance  $\theta_1$ ,  $\theta_2$  vary with  $r$  or  $\mathbf{L}_N$   
 $\Rightarrow$  Resonances **sweep** through parameter plane
- Time scales:  $t_{\text{orb}} \ll t_{\text{pr}} \ll t_{\text{GW}}$   
 $\Rightarrow$  "Free" binaries can get caught by resonance

# Evolution in $\theta_1, \theta_2$ plane for $q = 9/11$

$$\theta_i := \angle(\vec{S}_i, \vec{L}_N)$$

$$\theta_1 = \theta_2$$

$$\mathbf{S} \cdot \mathbf{L}_N = \text{const}$$

$$\mathbf{S}_0 \cdot \mathbf{L}_N = \text{const}$$

evolution

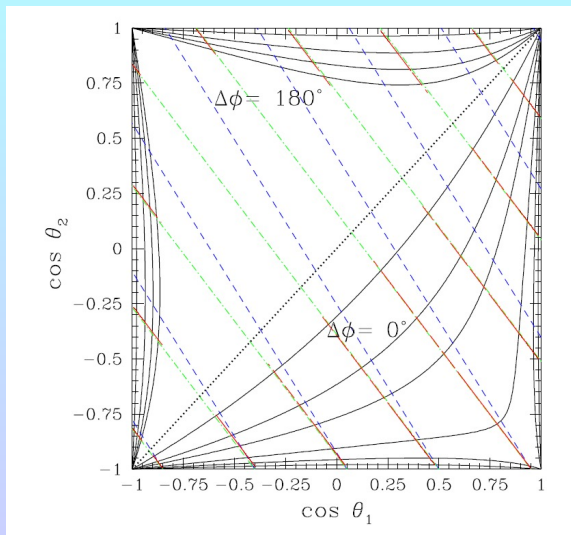
$\Rightarrow$  BHs approach

$$\theta_1 = \theta_2$$

$\Rightarrow$   $\mathbf{S}_1, \mathbf{S}_2$  align

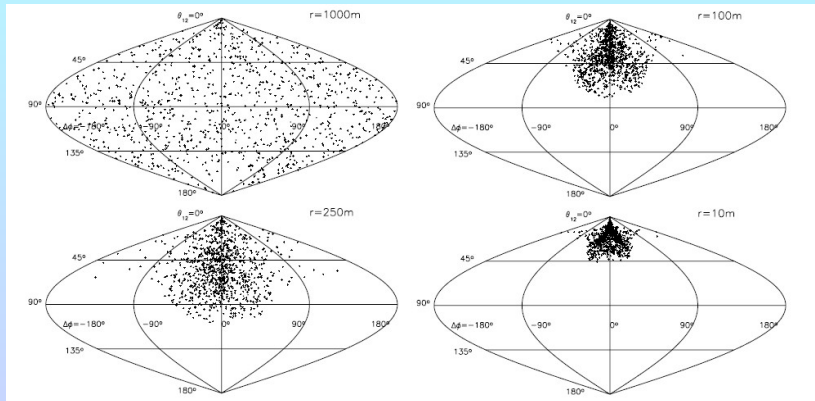
if  $\theta_1$  small

Kesden, US & Berti '10



# Resonance capture: $\Delta\phi = 0^\circ$

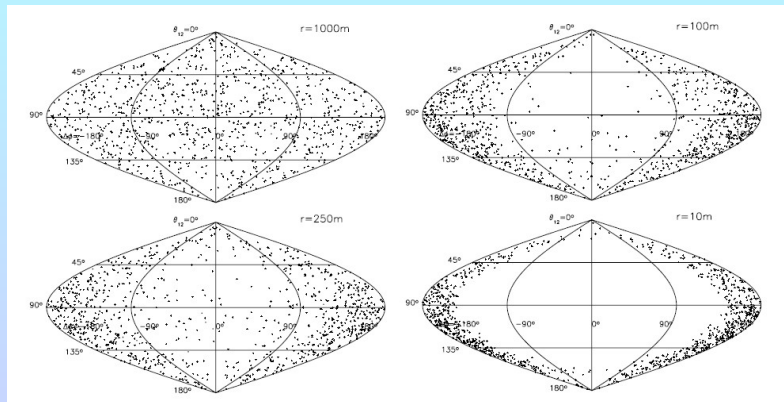
$q = 9/11$ ,  $\chi_i = 1$ ,  $\theta_1(t_0) = 10^\circ$ , rest random



Schnittman '04

# Resonance capture: $\Delta\phi = 180^\circ$

$q = 9/11$ ,  $\chi_i = 1$ ,  $\theta_1(t_0) = 170^\circ$ , rest random



Schnittman '04

# Consequences of resonances

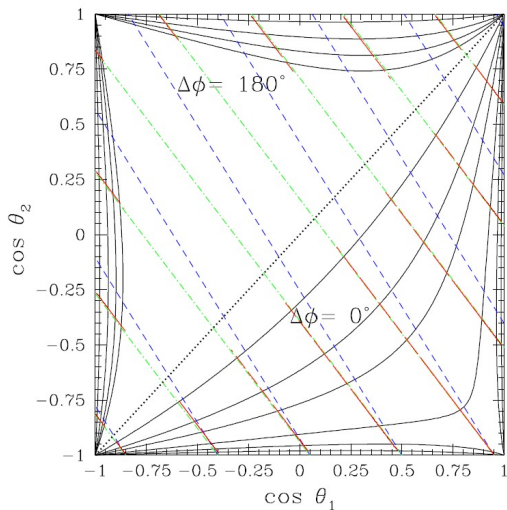
EOB spin

$$\mathbf{S}_0 = \frac{M}{m_1} \mathbf{S}_1 + \frac{M}{m_2} \mathbf{S}_2$$

$$\mathbf{S}_0 \cdot \mathbf{L}_N = \text{const}$$

evolution

$\Rightarrow \mathbf{S}_0 \sim \text{conserved}$



# Consequences of resonances

Total spin

$$\mathbf{S} = \mathbf{S}_1 + \mathbf{S}_2$$

$$\vec{S} \cdot \vec{L}_N = \text{const}$$

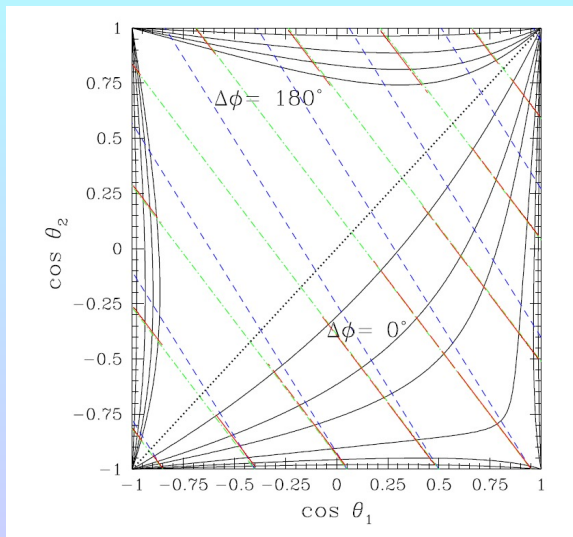
evolution

blue steeper red

$\Rightarrow \mathbf{S}, \mathbf{L}_N$  become

antialigned;  $\Delta\phi = 0^\circ$

aligned;  $\Delta\phi = 180^\circ$





# Consequences of resonances

$r$  decreases

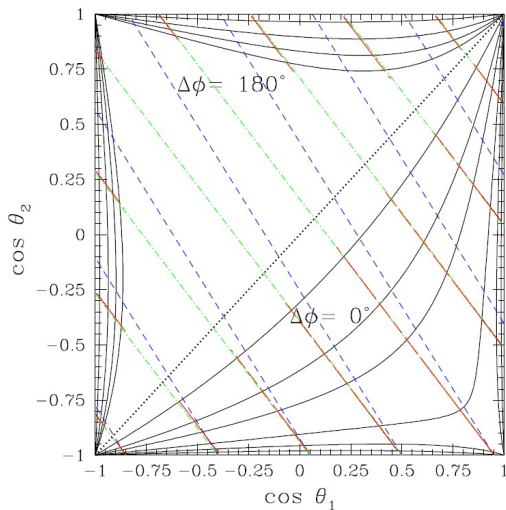
$\Rightarrow \theta_1, \theta_2 \rightarrow$  diagonal

i.e.  $\theta_1 = \theta_2$

$\Rightarrow \mathbf{S}_1, \mathbf{S}_2$  become

aligned;  $\Delta\phi = 0^\circ$

$\theta_{12} = \theta_1 + \theta_2$ ;  $\Delta\phi = 180^\circ$



# Summary: Resonances

- $\mathbf{S}_1$ ,  $\mathbf{S}_2$ ,  $\mathbf{L}_N$  precess in plane
- 2 types: I)  $\Delta\phi = 0^\circ$ , II)  $\Delta\phi = 180^\circ$
- Free binaries can get caught by resonances
- Consequences for  $\Delta\phi = 0^\circ$ 
  - $\mathbf{S}_1$ ,  $\mathbf{S}_2$  aligned
  - $\mathbf{S}$ ,  $\mathbf{L}_N$  antialigned
- Consequences for  $\Delta\phi = 180^\circ$ 
  - $\mathbf{S}_1$ ,  $\mathbf{S}_2$  approach  $\theta_{12} = \theta_1 + \theta_2$
  - $\mathbf{S}$ ,  $\mathbf{L}_N$  aligned

# 5. Suppression of superkicks

# Setup

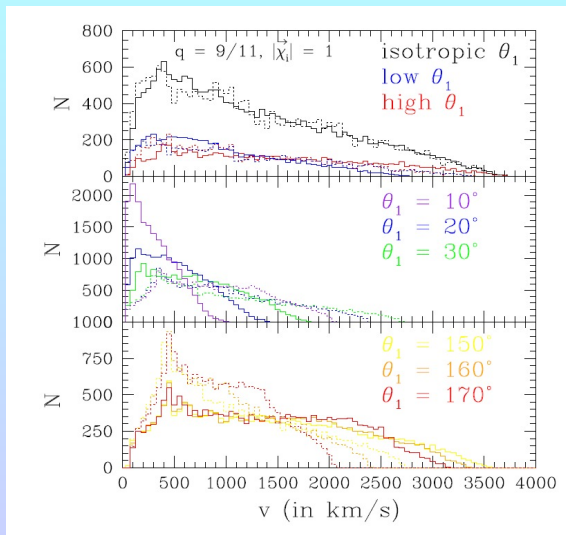
- BBHs inspiral from  $1000 M$  to  $10 M$
- Ensemble 1:  $10 \times 10 \times 10$  isotropic
- Ensemble 2:  $30 \times 30$  isotropic in  $\theta_2, \Delta\phi$   
fix  $\theta_1(t_0) = 170^\circ, 160^\circ, 150^\circ, 30^\circ, 20^\circ, 10^\circ$
- Map  $\mathbf{S}_1, \mathbf{S}_2, q$  to  $v_{\text{kick}}$

$$\vec{v}(q, \chi_1, \chi_2) = v_m \hat{\mathbf{e}}_1 + v_\perp (\cos \xi \hat{\mathbf{e}}_1 + \sin \xi \hat{\mathbf{e}}_2) + v_\parallel \hat{\mathbf{e}}_z$$

$$v_\parallel \sim |\Delta^\perp|, \quad \Delta = \frac{q\chi_2 - \chi_1}{1+q}$$

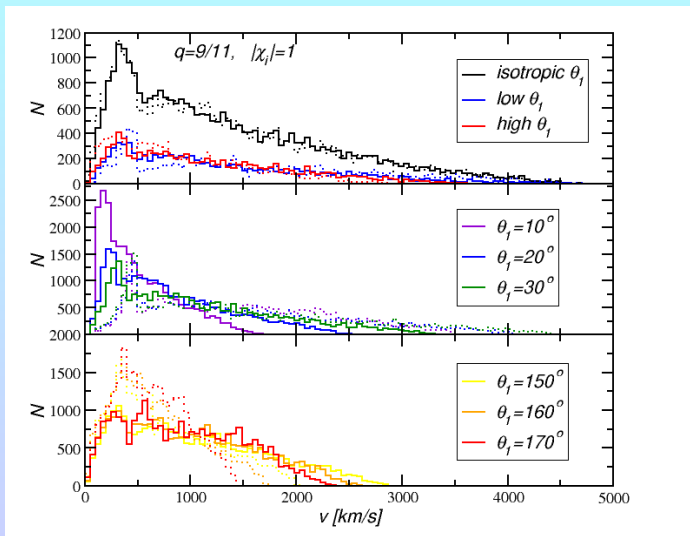
Campanelli, Lousto, Zlochower & Merritt '07

# Kick distributions with and without PN inspiral $q = \frac{9}{11}$



Kesden, US & Berti 2010

Same game for hang-up kicks:  $q = \frac{9}{11}$



Berti, Kesden & US 2012

## Summary: Kick suppression

- Resonances attract aligned (anti aligned) configurations towards  $\Delta\phi = 0^\circ$  ( $180^\circ$ )
- Superkicks suppressed (enhanced) for  $\Delta\phi = 0^\circ$  ( $\Delta\phi = 180^\circ$ ) resonances
- If accretion torque partially aligns  $\vec{S}_1$  with  $\vec{L}_N$   
 $\Rightarrow \Delta\phi = 0^\circ$  resonances dominate and suppress kicks
- Kick suppression still effective for hang-up kicks
- Why? Because the key angle is  $\Delta\phi$

# 6. Conclusions



# Conclusions

- Kicks important for many astrophysical scenarios  
BH ejection, BH populations, SMBH assembly, galaxy structure
- Kicks generate through asymmetry: mass ratio, spins
- Superkicks:  $v_{\text{kick}}$  up to 4 000 km/s , Hangup kicks: 5 000 km/s
- Kick formulae: apply to late inspiral
- Gas disks  $\Rightarrow$  spin alignment
- Spin-orbit resonances  
 $\Rightarrow$  change spin distribution  
 $\Rightarrow$  can suppress superkicks
- Open questions:  $q$  dependence, spin distribution