

Impact of structure on grazing collisions of black holes

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Overview

- Motivation
- Black-hole collisions in 3+1 dimensions
- Black-hole collisions in higher dimensional spacetimes
- Further topics
- Conclusions and outlook

1. Motivation

The Hierarchy Problem of Physics

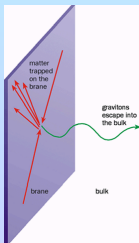
- Gravity $\approx 10^{-39} \times$ other forces
- Higgs field $\approx \mu_{obs} \approx 250 \text{ GeV} = \sqrt{\mu^2 - \Lambda^2}$
where $\Lambda \approx 10^{16} \text{ GeV}$ is the grand unification energy
- Requires enormous finetuning!!!
- Finetuning exist: $\frac{987654321}{123456789} = 8.0000000729$
- Or Planck mass is much lower?
I.e. Gravity much stronger at small length scales?
- Gravity not measured below 0.16 mm! Diluted due to...
 - Large extra dimensions
 - Extra dimension with warp factor

TeV Gravity

Large extra dimensions

Arkani-Hamed, Dimopoulos & Dvali '98

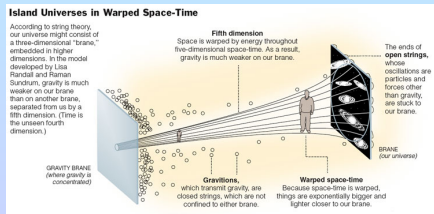
- SM confined to “3+1” brane
 - Gravity lives in bulk
- ⇒ Gravity diluted



Warped geometry

Randall & Sundrum '99

- 5D AdS Universe with 2 branes:
- “our” 3+1 world, gravity brane
- 5th dimension warped
- ⇒ Gravity weakened

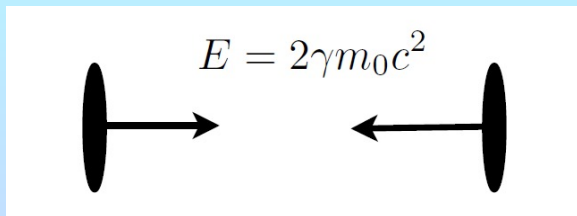


Either way: Gravity strong at $\gtrsim TeV$

BH formation and hoop conjecture

- Hoop conjecture

Thorne '72



- de Broglie wavelength: $\lambda = \frac{hc}{E}$

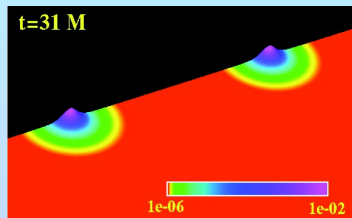
- Schwarzschild radius: $r = \frac{2GE}{c^4}$

- BH will form if $\lambda < r \Leftrightarrow E \gtrsim \sqrt{\frac{hc^5}{G}} \equiv E_{\text{Planck}}$

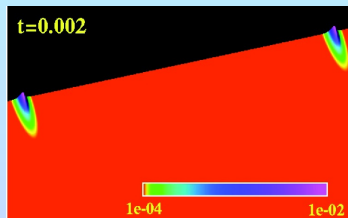
BH formation in boson field collisions

Pretorius & Choptuik '09

- Einstein plus minimally coupled, massive, complex scalar field
“Boson stars”



$$\gamma = 1$$



$$\gamma = 4$$

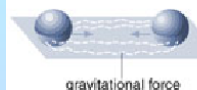
- BH formation threshold: $\gamma_{\text{thr}} = 2.9 \pm 10 \%$
- About 1/3 of hoop conjecture prediction

Motivation (High-energy physics)

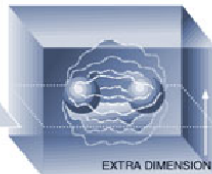
Black Holes on Demand

Scientists are exploring the possibility of producing miniature black holes on demand by smashing particles together. Their plans hinge on the theory that the universe contains more than the three dimensions of everyday life. Here's the idea:

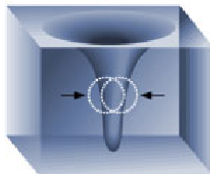
Particles collide in three dimensional space, shown below as a flat plane.



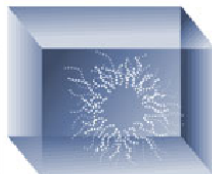
As the particles approach in a particle accelerator, their gravitational attraction increases steadily.



When the particles are extremely close, they may enter space with more dimensions, shown above as a cube.



The extra dimensions would allow gravity to increase more rapidly so a black hole can form.



Such a black hole would immediately evaporate, sending out a unique pattern of radiation.

- Matter does not matter at energies well above the Planck scale
⇒ Model particle collisions by black-hole collisions

Banks & Fischler '99;

Giddings & Thomas '01

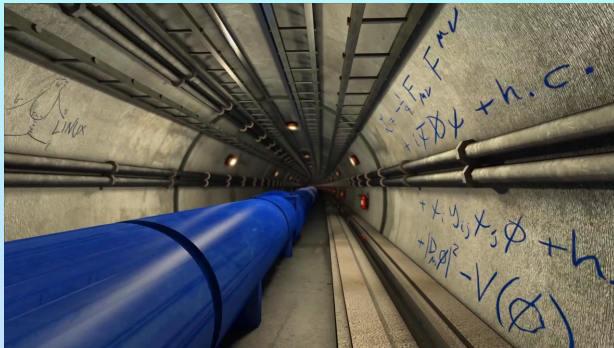
Black-hole formation in high-energy collisions

- Cosmic-rays hitting the earth's atmosphere
- Parton-parton collisions above TeV energies, LHC



→ Talk by Colon, Sec. R9

Proton collisions at the LHC



Energy stored in a single beam:

$360 \text{ MJ} = 90 \text{ kg}$ of TNT

$= 15 \text{ kg}$ of chocolate

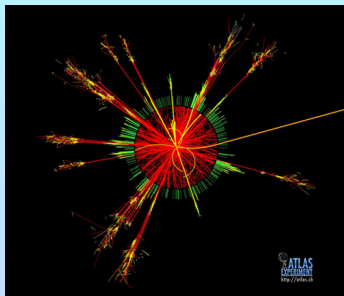
Landsberg '11 talk at NRHEP Madeira



Experimental signature at the LHC

Black hole formation at the LHC could be detected by the properties of the jets resulting from Hawking radiation.

- Multiplicity of partons: Number of jets and leptons
- Large transverse energy
- Black-hole mass and spin are important for this!



ToDo:

- Exact cross section for BH formation
- Determine loss of energy in gravitational waves
- Determine spin of merged black hole

Further motivation

BH collisions and dynamics of interest beyond TeV gravity:

- Test Cosmic Censorship
- Probe GR in the most violent regime
- Zoom-whirl behaviour; “critical” phenomena
- Super-Planckian physics?
- Collisions in alternative theories of gravity

2. Computational framework dimensions

Black-hole collisions in $D = 4$

- Numerical relativity breakthroughs carry over
Pretorius '05, Goddard '05, Brownsville-RIT '05
- “Moving puncture” technique
- **BSSN** formulation; Shibata & Nakamura '95, Baumgarte & Shapiro '98
- $1 + \log$ slicing, Γ -driver shift condition
- Puncture ini-data; Bowen-York '80; Brandt & Brügmann '97; Ansorg et al. '04
- Mesh refinement *Cactus*, *Carpet*
- Wave extraction using **Newman-Penrose scalar**
- **Apparent Horizon** finder; e.g. Thornburg '96

Black-hole collisions in $D = 4$

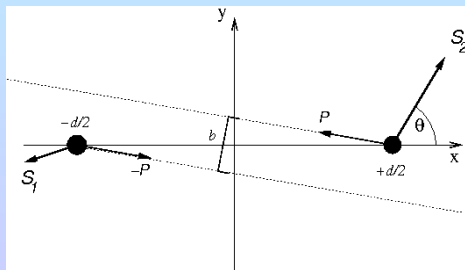
- Take two black holes

Total rest mass: $M_0 = M_{A,0} + M_{B,0}$

Initial position: $\pm x_0$

Linear momentum: $\mp P[\cos \alpha, \sin \alpha, 0]$

- Impact parameter: $b \equiv \frac{L}{P}$

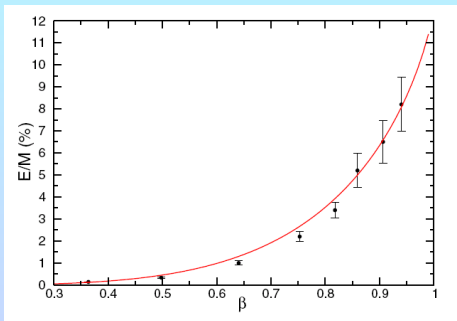


3. The non-spinning case

Head-on collisions: $b = 0$, $\vec{S} = 0$

- Total radiated energy: $14 \pm 3 \%$ for $\nu \rightarrow 1$ US *et al.* '08

About half of Penrose '74



- Agreement with approximative methods

Flat spectrum, multipolar GW structure

Berti *et al.* '10

$b \neq 0$: Zoom whirl orbits

Pretorius & Khurana '07

- 1-parameter family of initial data: impact parameter

- Fine tune parameter

⇒ “Threshold of
immediate merger”

- Analogue in geodesics

- Reminiscent of

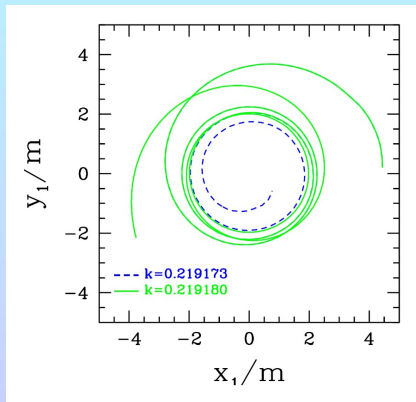
“Critical Phenomena”

- Similar observations by

Healy *et al.* '09

Zoom-whirl more likely for

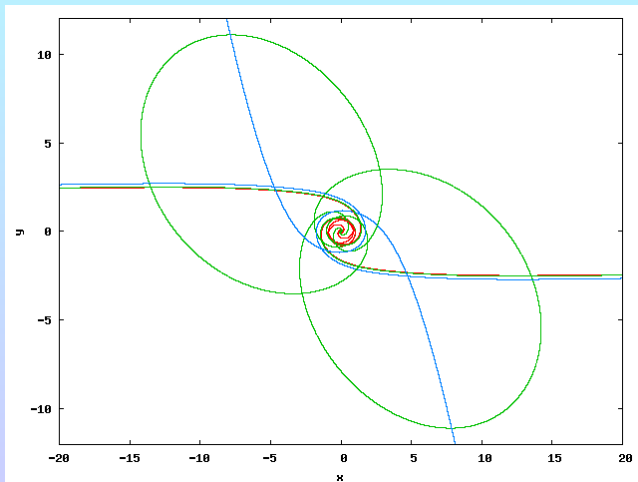
larger q



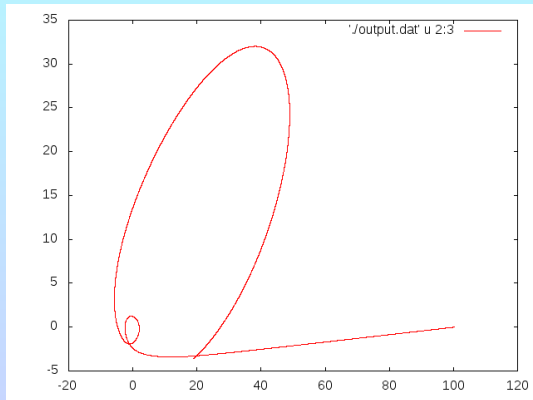
Grazing collisions: $b \neq 0$, $\vec{S} = 0$, $\gamma = 1.52$

Immediate vs. Delayed vs. No merger

US, Cardoso, Pretorius, Berti, Hinderer & Yunes '09



Grazing collisions: $b = 2.55 M$, $\vec{S} = 0$, $\gamma = 2.68$



Critical impact parameter

● $b < b_{\text{crit}} \Rightarrow$ Merger

$b > b_{\text{crit}} \Rightarrow$ Scattering

● Numerical study: $b_{\text{crit}} = \frac{2.5 \pm 0.05}{v} M$

Shibata, Okawa & Yamamoto '08

● Independent study by US, Pretorius, Cardoso, Berti *et al.* '09, '12

$\gamma = 1.23 \dots 2.93$:

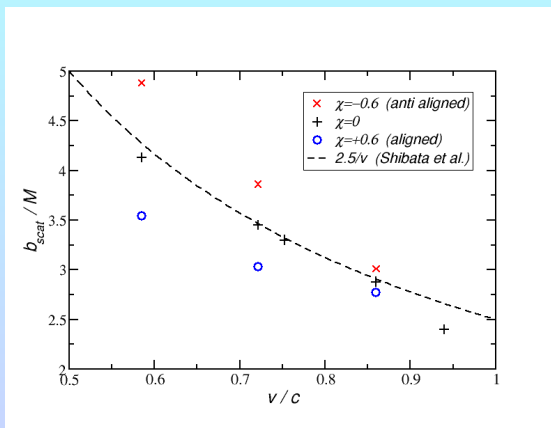
$\chi = -0.6, 0, +0.6$ (anti-aligned, nonspinning, aligned)

● Limit from Penrose construction: $b_{\text{crit}} = 1.685 M$

Yoshino & Rychkov '05

Critical impact parameter

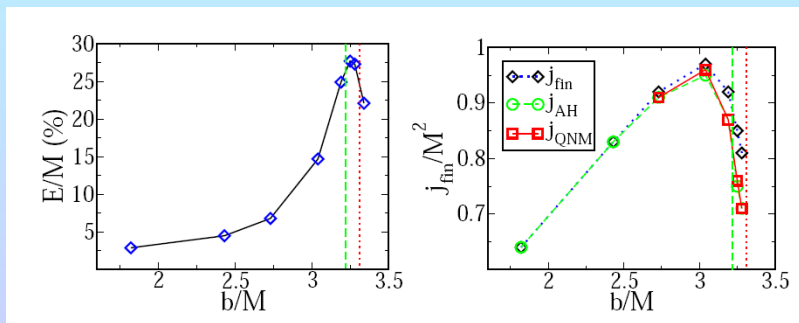
Preliminary results



- Effect of spin reduced for large γ
- b_{scat} for $v \rightarrow 1$ not quite certain

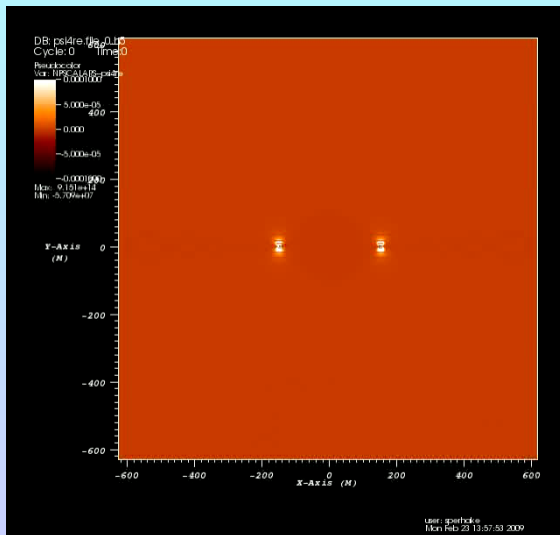
Radiated quantities

- b -sequence with $\gamma = 1.52$
- Final spin close to Kerr limit
- $E_{\text{rad}} \sim 35\%$ for $\gamma = 2.93$; about 10% of Dyson luminosity



US, Cardoso, Pretorius, Berti, Hinderer & Yunes '09

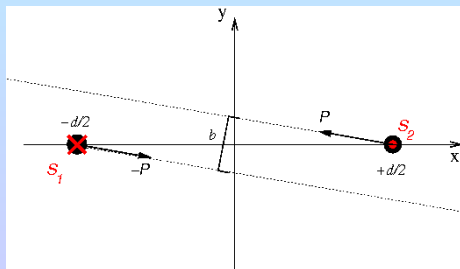
Gravitational radiation: Delayed merger



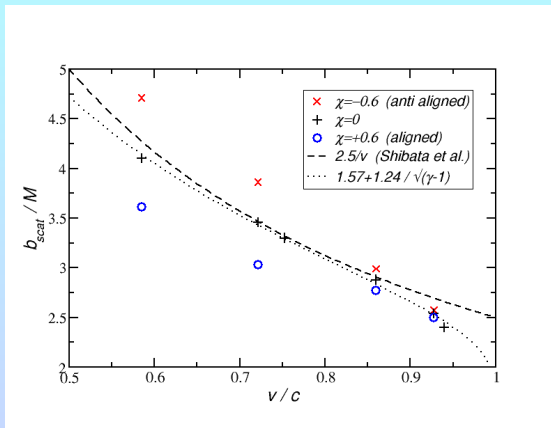
4. Collisions of spinning holes

Initial configurations

- Mass ratio $q = 1$
- Impact parameter: $b \equiv \frac{L}{P}$
- Equal spins $\vec{S}_1 = \vec{S}_2$ aligned or anti-aligned with \vec{L}
- Spin magnitude $\chi_i = |\vec{S}_i|/M_i^2 = 0.63$
- Three sequences 'a', 'n', 'aa' for $\gamma = 1.233, 1.444, 1.958, 2.679$



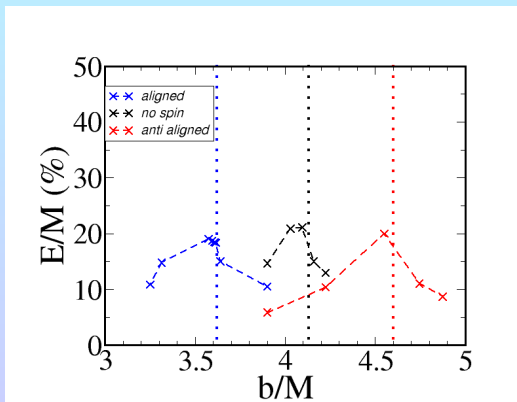
Diminishing impact of structure as $v \rightarrow 1$



- Effect of spin reduced for large γ
- b_{scat} for $v \rightarrow 1$ not quite certain

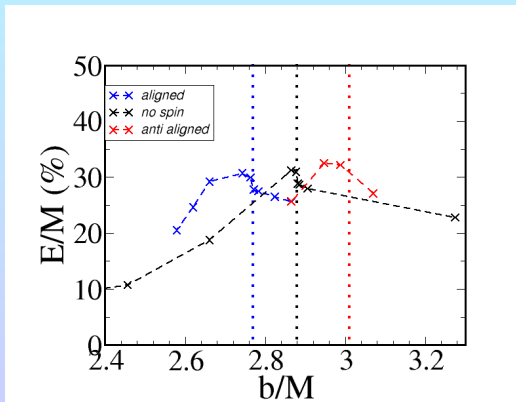
Radiated GW energy: $\gamma = 1.23$

- $\chi_{1,2} = 0, \pm 0.6$
- Vary b
- “Hang-up” has little impact on radiation



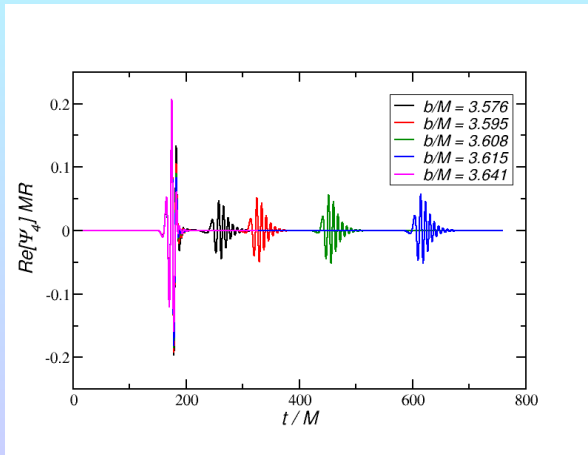
Radiated GW energy: $\gamma = 1.96$

- $\chi_{1,2} = 0, \pm 0.6$
- Vary b
- Relatively minor increase in E_{rad}



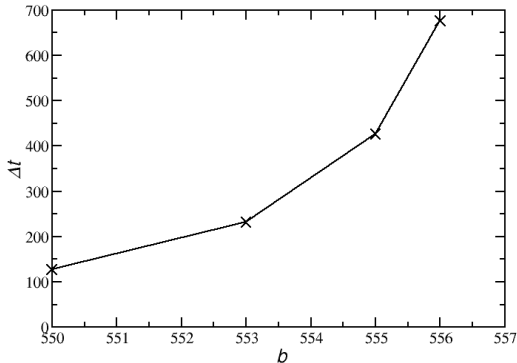
Delayed mergers: Aligned case, $\gamma = 1.52$

- Delayed merger \Rightarrow Two wave bursts
- $b \rightarrow b_{scat} \Rightarrow \text{Gap} \rightarrow \infty$



Delayed mergers: Aligned case, $\gamma = 1.52$

- Delayed merger \Rightarrow Two wave bursts
- $b \rightarrow b_{scat} \Rightarrow \text{Gap} \rightarrow \infty$



5. Conclusions

Conclusions

- “3+1” numerical framework can be modified for higher D
- Stability not yet as robust as in $D = 4$; gauge?
- Scattering threshold in 4D: $b_{\text{crit}} \approx \frac{2.5 M}{v}$
- Cosmic Censorship holds
- Zoom-whirl behaviour in 4D
- Impact of spin diminishes as γ increases
- Maximal GW energy little affected by spin
- Delay $\rightarrow \infty$ as $b \rightarrow b_{\text{scat}}$; Universal scaling?