

11 Orbit inspiral of unequal-mass BHBs

U. Sperhake

CSIC-IEEC Barcelona
California Institute of Technology
University of Mississippi
FSU Jena

Capra/NRDA, Waterloo, 24th June 2010

B. Brügmann, D. Müller,
E. Berti, M. Kesden



U. Sperhake (CSIC-IEEC)



11 Orbit inspiral of unequal-mass BHBs



“These go to eleven”



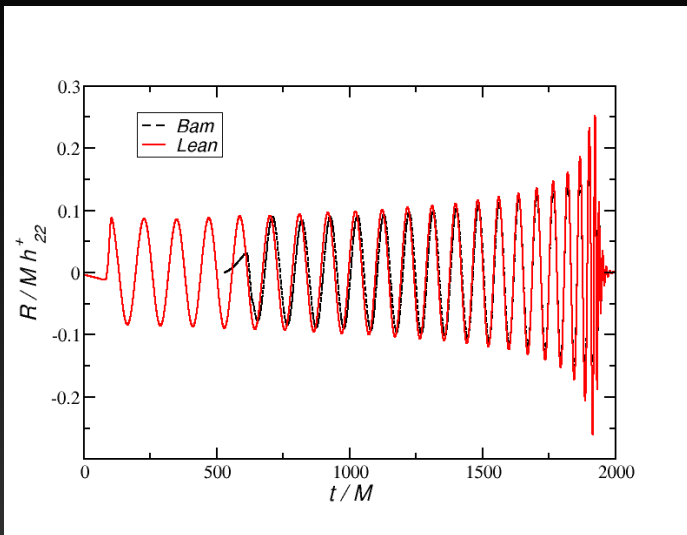
Motivation

- Obtain *accurate, long* waveforms for unequal mass ratios for use in GW DA
- Comparison with alternative codes
- Matching to PN
- Calibrate accuracy: convergence, extraction radius, eccentricity
- Study non-dominant multipoles
- Optimize efficiency

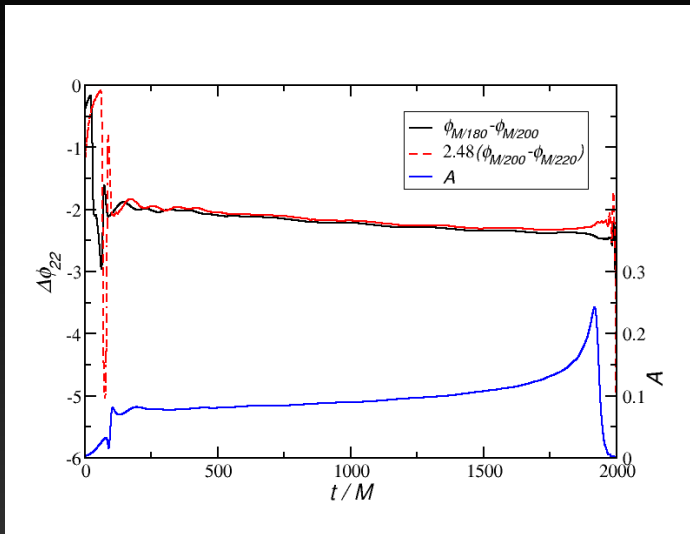
Binary parameters

- mass ratio $q = 4$
- initial orbital frequency $M\omega = 0.05$
- grid setup:
 $\{(307.2, 153.6, 102.4, 32, 16) \times (3.2, 1.6, 0.8, 0.4, 0.2), h\}$
 $h = M/180, M/200, M/220, M/240$
- extraction radii: $R_{ex} = 56, 64, 72, 80, 88, 96, 104, 112 M$
- gauge: $\partial_t \alpha = \beta^m \partial_m \alpha - 2\alpha K$
 $\partial_t \beta^i = \beta^m \partial_m \beta^i + \frac{3}{4} \tilde{\Gamma}^i - \eta \beta^i$
 $M\eta = 1.75$

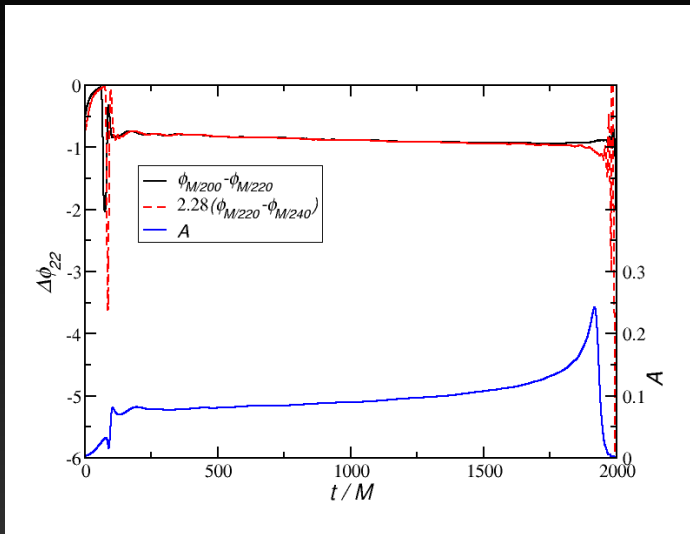
BAM, LEAN waveforms



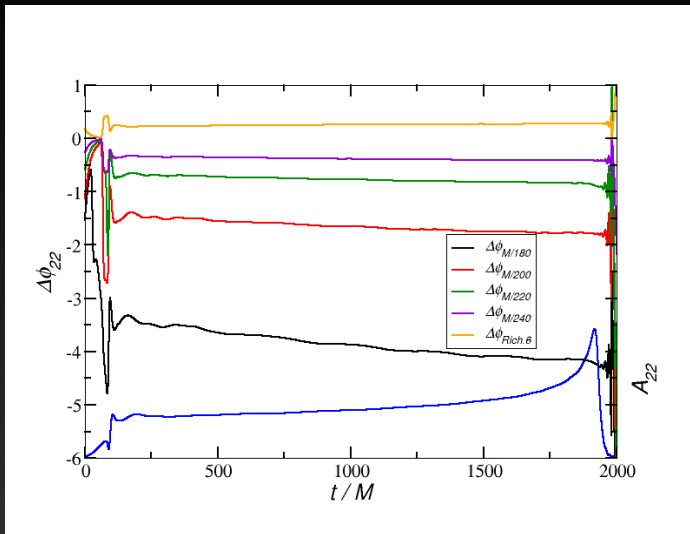
Convergence of $\ell = 2, m = 2$ mode: Phase



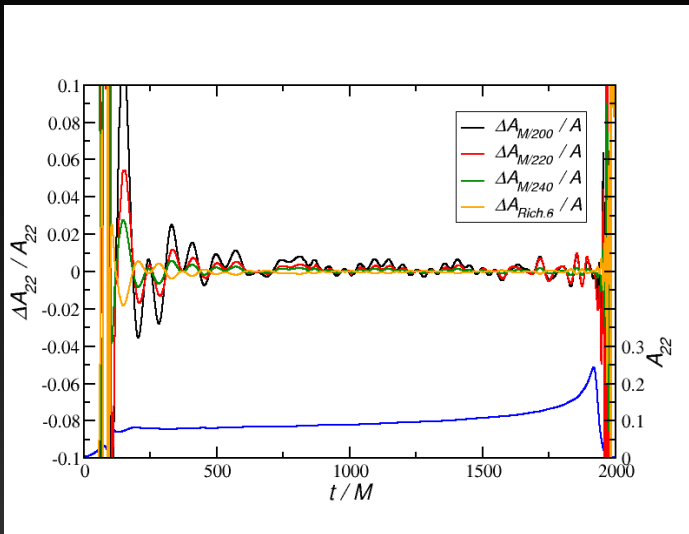
Convergence of $\ell = 2, m = 2$ mode: Phase



Convergence of $\ell = 2, m = 2$ mode: Phase



Convergence of $\ell = 2, m = 2$ mode: Amplitude



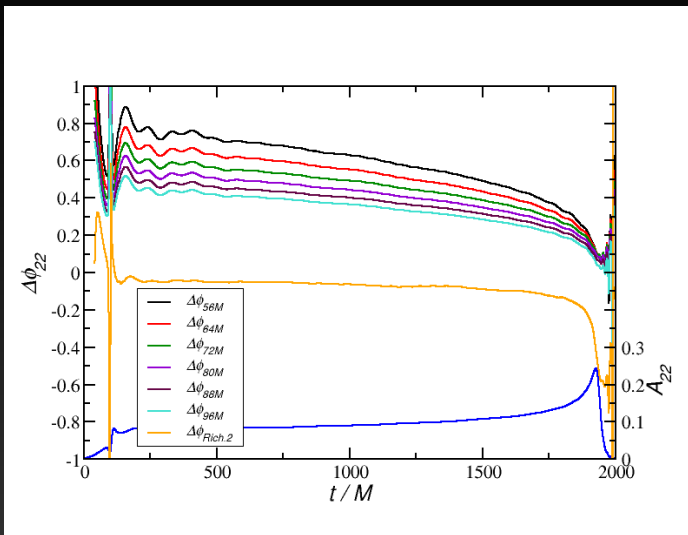
Discretization errors: summary

- $R_{\text{ex}} = 88 M$
- $\Delta\phi_{22} \approx 0.2 \text{ rad}$
- $\Delta A_{22}/A_{22} \approx 0.5 \%$
- little variation over $t \approx 250 M \dots 2000 M$
- Errors larger during first orbits, late ringdown

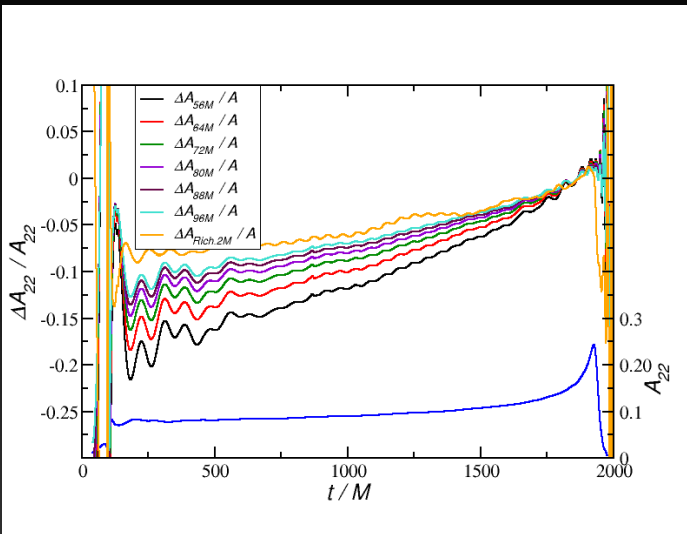
Error due to extraction radius

- Fix $h = M/240$
- $R_{\text{ex}} = 56M, 64M, 72M, 80M, 88M, 96M$
- Extrapolate assuming $f = f_0 + f_1/r$
or $f = f_0 + f_1/r + f_2/r^2$
- Use f_0 as estimate at infinity
- **Caution:** Do not use underresolved extraction radii!
Amplitudes would be contaminated due to dissipation.

Extraction of $\ell = 2, m = 2$ mode: Phase



Extraction of $\ell = 2, m = 2$ mode: Amplitude



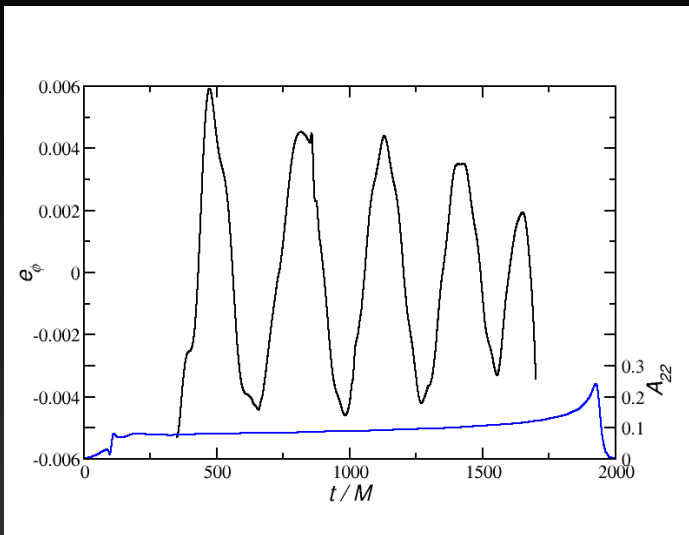
Extraction errors: summary

- $h = M/240$
- $\Delta\phi_{22} \lesssim 0.2$ rad
- $\Delta A_{22}/A_{22} \approx 10\text{...}1$ %
- little variation in $\Delta\phi$ over $t \approx 250 M \dots 2000 M$
- Amplitude errors larger during first orbits, late ringdown

Eccentricity

- Use GW phase of $\ell = 2, m = 2$ mode
- $h = M/240$
- $R_{\text{ex}} = 96 M$
- $e_\phi(t) = \frac{\phi_{\text{NR}}(t) - \phi_{\text{fit}}(t)}{4}$
Mroué, Pfeiffer, Kidder & Teukolsky (2010)
- Fit 7th-order polynomial
- Time window: $t = 350 \dots 1700 M$

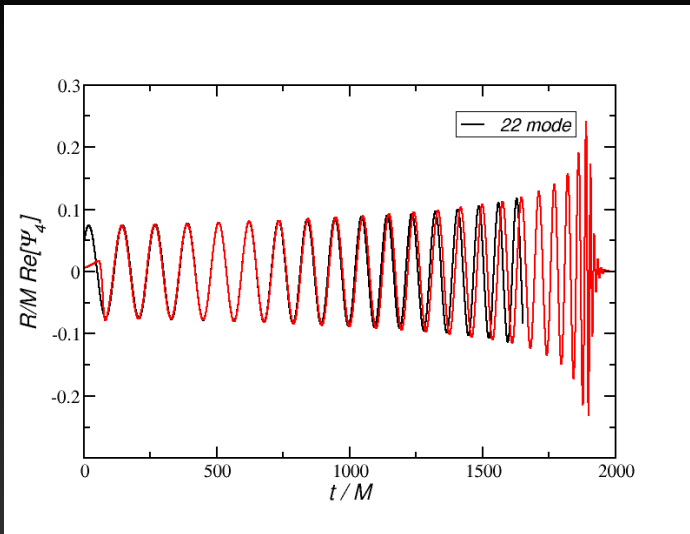
Eccentricity



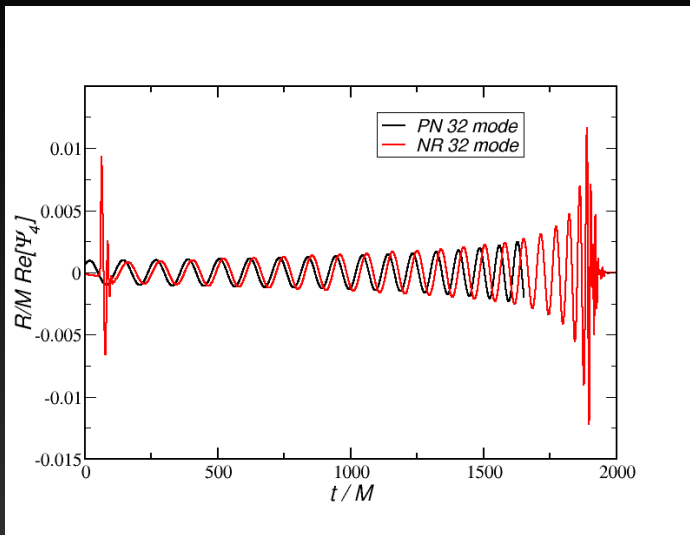
PN hybridization

- $\ell = 2, m = 2$ and $\ell = 3, m = 2$ modes
- $h = M/240$
- Taylor T1, e. g. Boyle *et al.* PRD 76, 124038 (2007)
Phasing: Blanchet, Liv. Rev. 4, 9 (2006)
Amplitudes: Kidder, PRD 77, 044016 (2008)
- Maximize overlap of $\ell = 2, m = 2$ multipole using
Downhill Simplex Method
- **Note:** This fixes the phase for **all** modes!
- Time window: $t = 350 \dots 700 M$

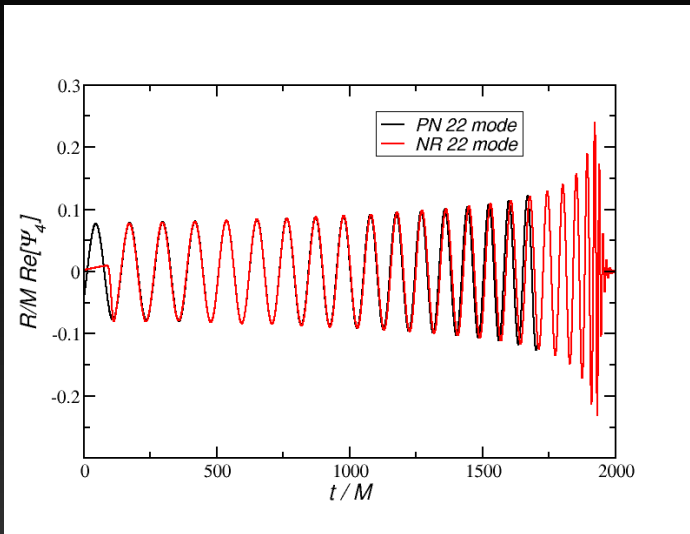
$R_{\text{ex}} = 56 M$: PN hybridization $\ell = 2, m = 2$



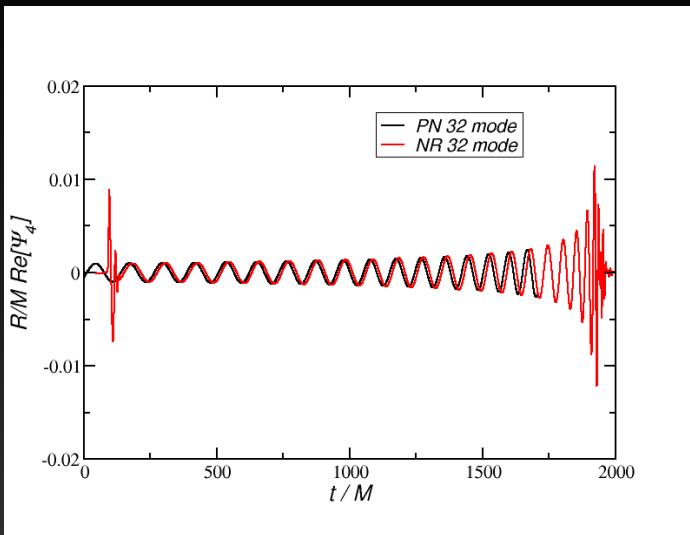
$R_{\text{ex}} = 56 M$: PN hybridization $\ell = 3, m = 2$



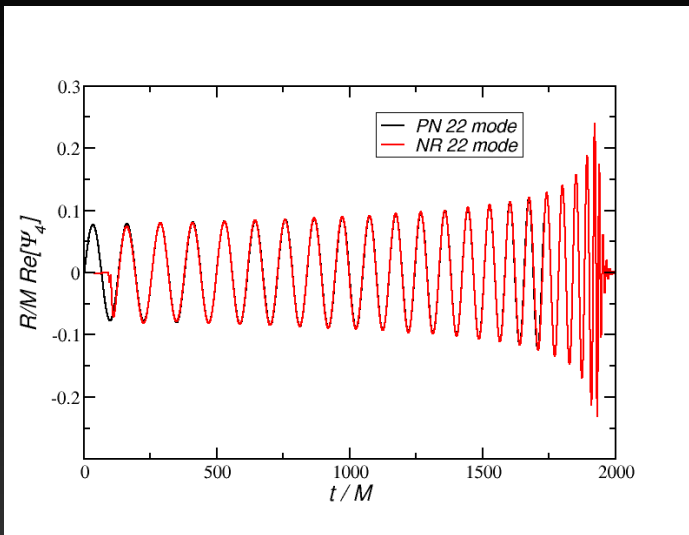
$R_{\text{ex}} = 96 M$: PN hybridization $\ell = 2, m = 2$



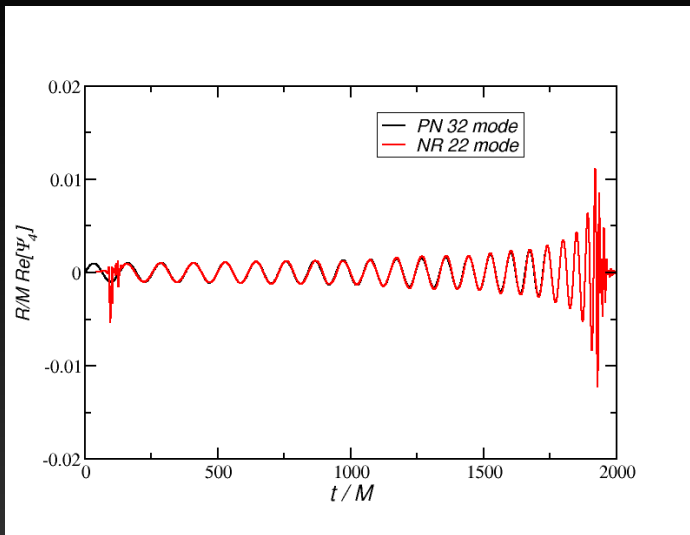
$R_{\text{ex}} = 96 M$: PN hybridization $\ell = 3, m = 2$



$R_{\text{ex}} \rightarrow \infty$: PN hybridization $\ell = 2, m = 2$



$R_{\text{ex}} \rightarrow \infty$: PN hybridization $\ell = 3, m = 2$



Conclusions

- $q = 4$ binary
- Discretization: $\Delta\phi_{22} \approx 0.2$ rad, $\Delta A_{22}/A_{22} \approx 0.5$ %
- Extraction radius: $\Delta\phi_{22} \lesssim 0.2$ rad, $\Delta A_{22}/A_{22} \approx 10..1$ %
- Eccentricity: $e_\phi \approx 5 \times 10^{-3}$
- Hybridization: xpol $R_{\text{ex}} \rightarrow \infty$ required for ℓ , $m = 2$

Suppression of superkicks

- Numerical Relativity predicts kicks of $\sim 10^3$ km/s
- Larger than escape velocities of even the most massive galaxies
- Galaxies ubiquitously harbor BHs
- How come they are not kicked out in mergers?

- Partial alignment of S_1 , L

Bogdanović *et al.*, ApJ 661, L147 (2007)

Dotti *et al.*, MNRAS 402, 682 (2010)

- PN evolution from $R = 1000 M$ on

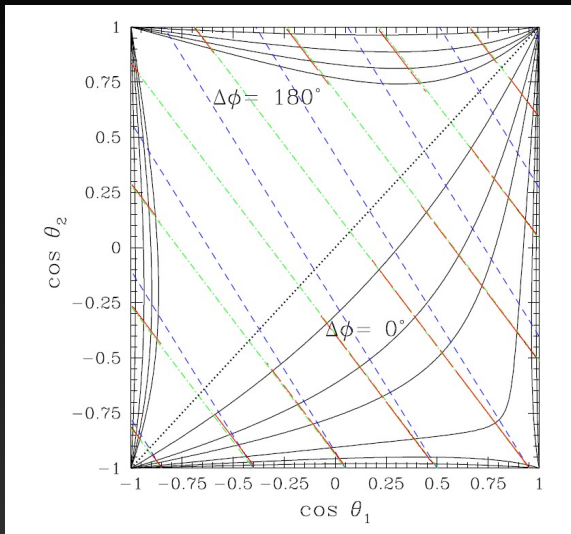
Kesden, Sperhake & Berti, PRD 81, 084054 (2010)

Kesden, Sperhake & Berti, ApJ 715, 1006 (2010)

PN evolution

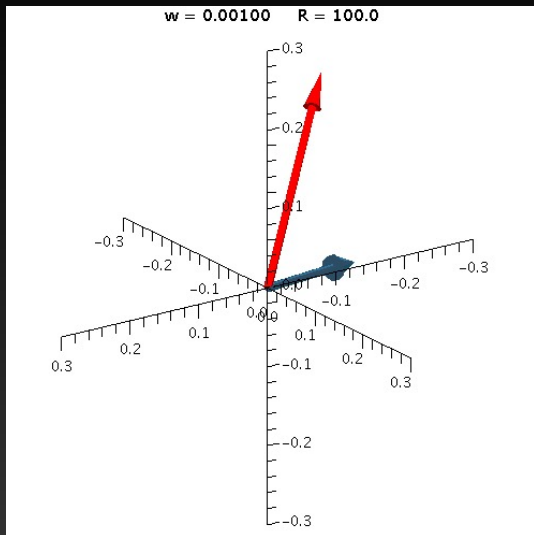
- PN equations of motion for precessing, qc BBHs
Kidder, PRD 52, 821 (1995)
- Quadrupole-monopole interaction
Poisson, PRD 57, 5287 (1997)
- Spin-spin interaction
Mikoczi, Vasuth & Gergely, PRD 71, 124043 (2005)
- Adaptive stepsize integrator STEPPERDOPR5

Evolution in θ_1, θ_2 plane



Time evolution of \vec{S}_1, \vec{S}_2

$$\theta_1 = 10^\circ, \theta_2 = 154^\circ, \Delta\phi = 264^\circ$$



Kick distributions with and without PN inspiral

