### **SPH simulations of galaxy formation**

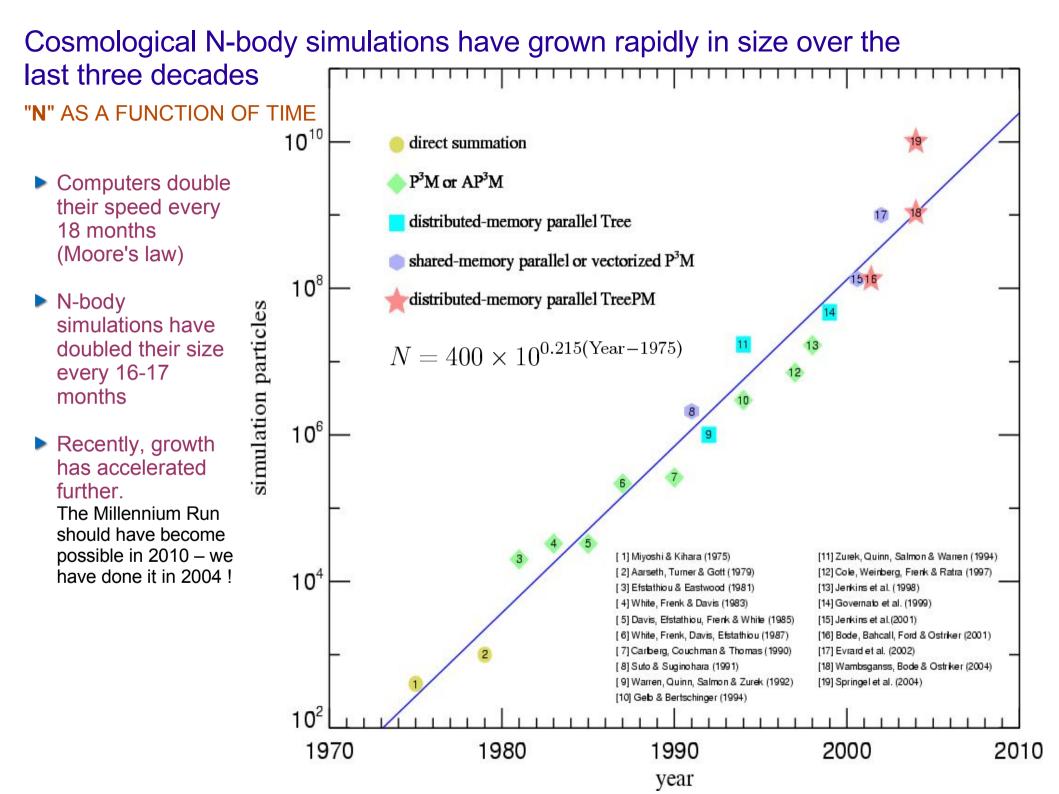
Looking under the hood of GADGET-2

Volker Springel

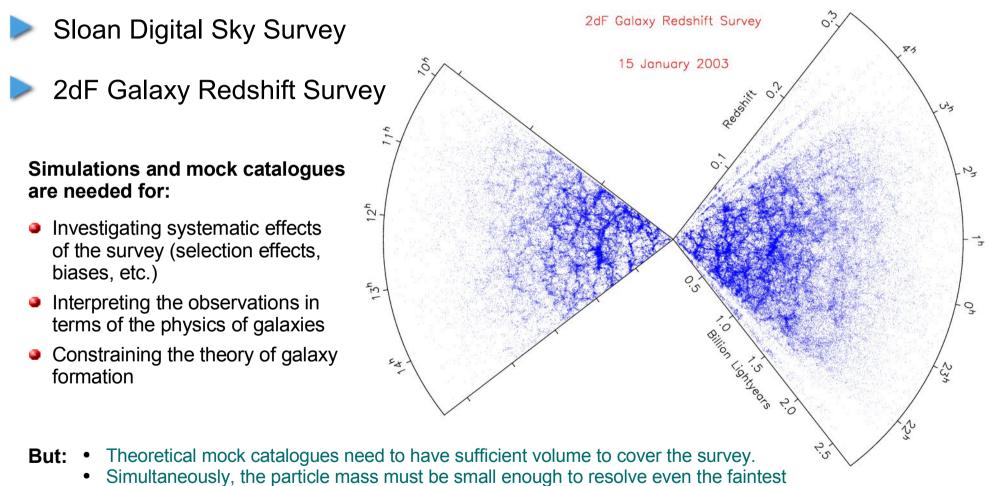
- Large N-body runs
- Algorithmic aspects of a new simulation code: GADGET- II
- Non-standard physics in simulations of galaxy formation
  - sub-resolution multiphase-model for star formation, feedback & galactic winds
  - accretion on SMBH and feedback







Full exploitation of large observational galaxy surveys relies on theoretical mock catalogues of adequate size EXAMPLES OF CURRENT OBSERVATIONAL SURVEYS

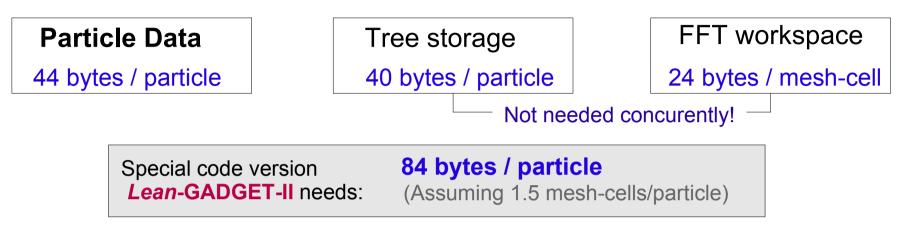


galaxies that enter the survey.

Thanks to its extremely large dynamic range, the Millennium Run meets the opposing requirements of large volume and small particle mass like no other simulation before.

### The maximum size of a TreePM simulation with *Lean*-GADGET-II is essentially memory bound

A HIGHLY MEMORY EFFICIENT VERSION OF GADGET-II



#### Simulation Set-up:

- Particle number:  $2160^3 = 10.077.696.000 = \sim 10^{10}$  particles
- Boxsize:  $L = 500 h^{-1} Mpc$
- Particle mass:  $m_p = 8.6 \times 10^8 h^{-1} M_{\odot}$
- Spatial resolution: 5 h<sup>-1</sup> kpc
- Size of FFT: 2560<sup>3</sup> = 16.777.216.000 = ~ 17 billion cells

Compared to Hubble-Volume simulation:

> 2000 times better mass resolution

Minimum memory requirement

of simulation code

~840 GByte

- 10 times larger particle number
- 13 better spatial resolution

# The simulation was run on the *Regatta* supercomputer of the RZG REQUIRED RESSOURCES

#### 1 TByte RAM needed

16 X <sup>32-way Regatta Node</sup> **64 GByte RAM** 512 CPU total

#### CPU time consumed 350.000 processor hours

- 28 days on 512 CPUs/16 nodes
- 38 years in serial
- ~ 6% of annual time on total Regatta system
- sustained average code performance (hardware counters) 400 Mflops/cpu
- 5 x 10<sup>17</sup> floating point ops
- 11000 (adaptive) timesteps



#### The simulation produced a multi-TByte data set RAW SIMULATION OUTPUTS

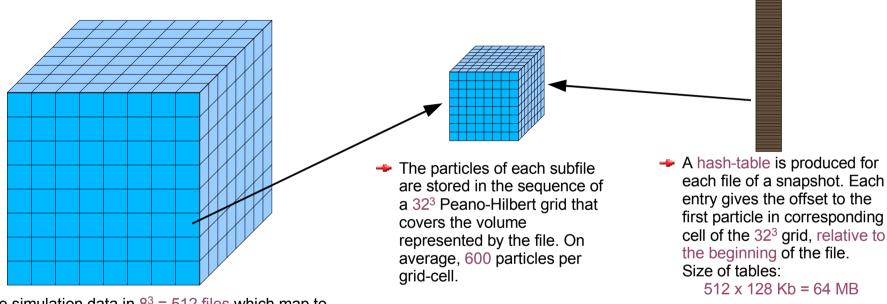
Data size

One simulation timeslice **360 GByte** 

we have stored 64 outputs

Raw data volume **23 TByte** 

#### Design for structure of snapshot files



- Store simulation data in 8<sup>3</sup> = 512 files which map to subcubes in the simulation volume.
- Each file has ~ 20 million particles, 600 MB.

#### FoF group catalogues

Are computed on the fly

 Group catalogue: Length of each group and offset into particle list

 Long list of particle keys (64 bit) that make up each group Structure of 64-bit particle key
 Structure of 64-bit particle key
 9 bit 34 bit
 Hash-Key File-Key Particle-ID

Allows random access to

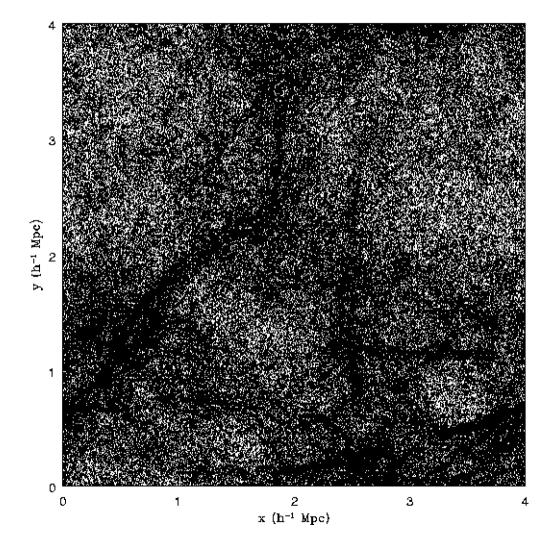
particle data of subvolumes.

 Allows fast selective access to all particles of a given group Visualization of large particle simulation data sets is challenging THE TRADITIONAL DOT-PLOT IS STILL USED BY A NUMBER OF GROUPS

astro-ph (2004)

512<sup>3</sup> particles

4  $h^{-1}$ Mpc boxsize



0.25% of particles projected onto xy-plane

1 Gpc/h

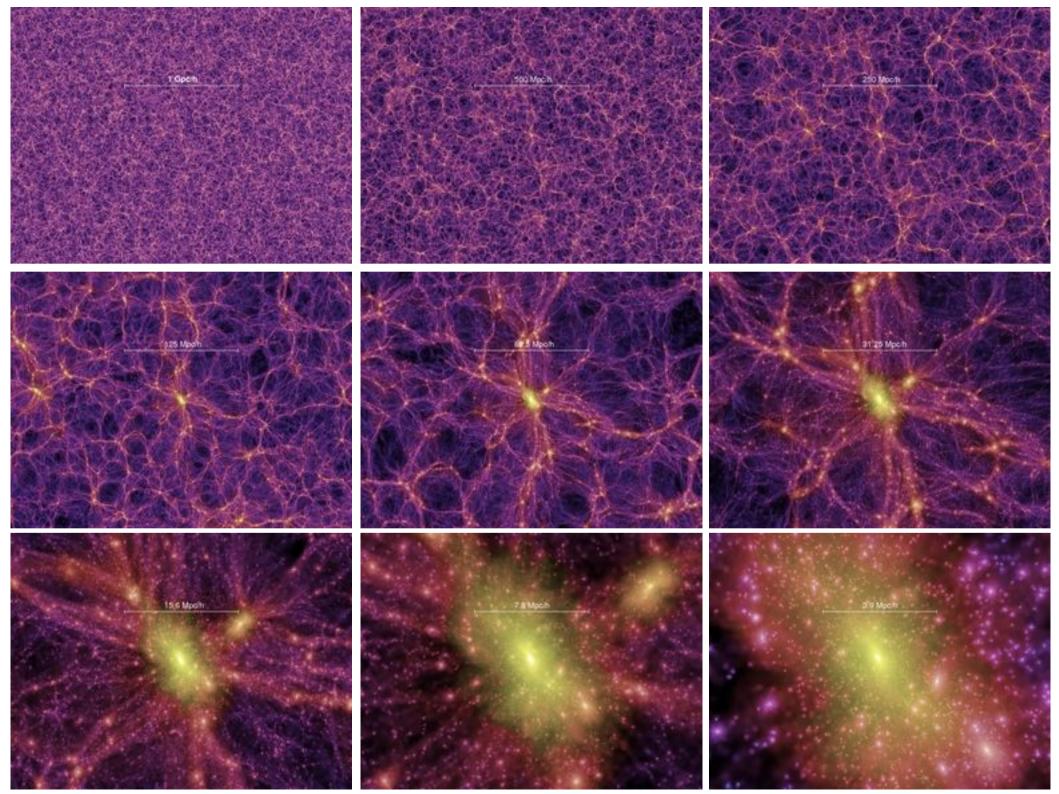
### Millennium Run 10.077.960.000 particles

Springel et al. (2004)

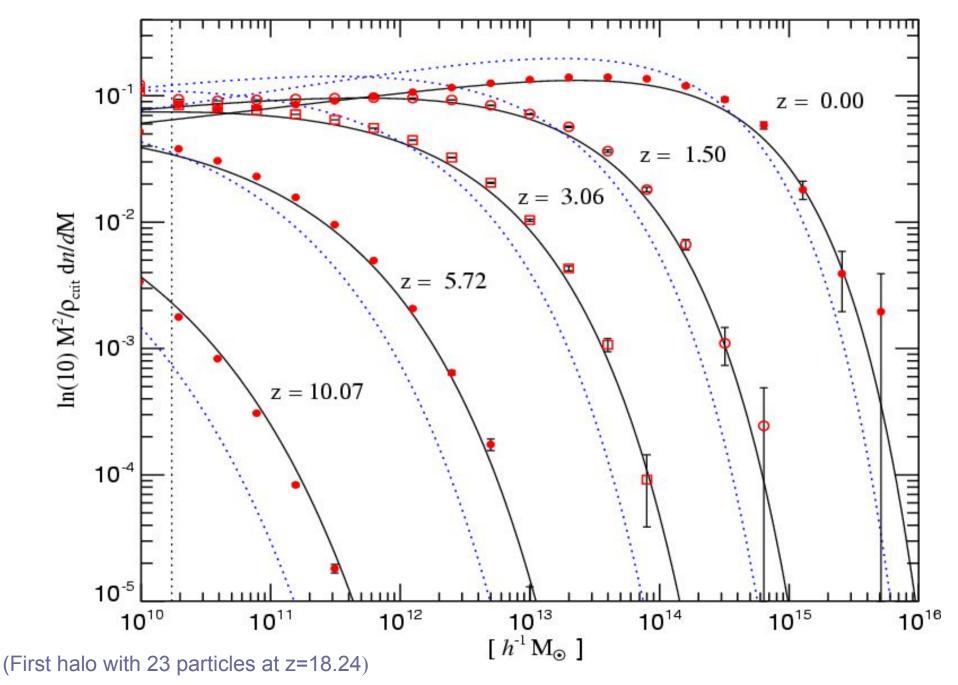


Max-Planck Institut für Astrophysik





The halo mass function is very well fit by the model of Sheth & Tormen MASS MULTIPLICITY FUNCTION



The non-linear 4 evolution of the mass power z = 0.00spectrum is accurately determined by 2 the Millennium Run over a large range of scales MASS POWER  $\Delta^{2}(k)$ SPECTRUM 0 z = 14.87 -2 1111 0.01 0.10 1.00 10.00

z = 0.98

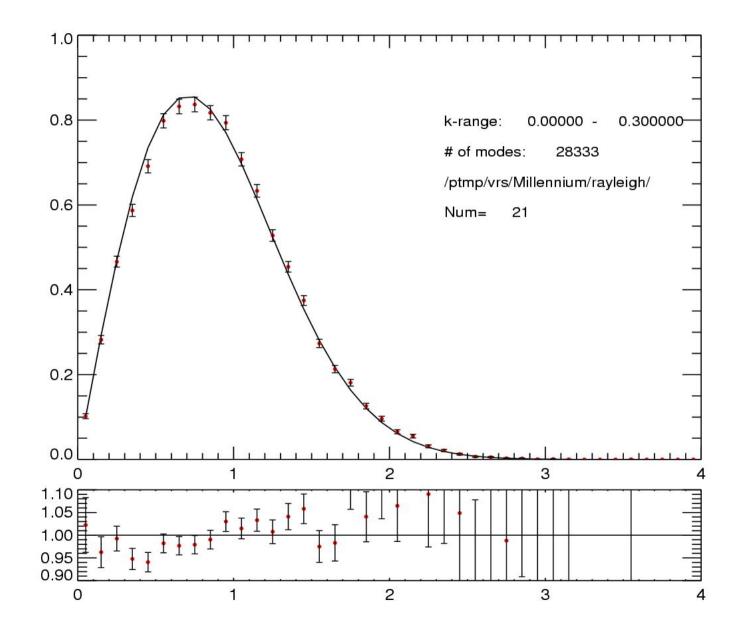
z = 7.02

k [h / Mpc]

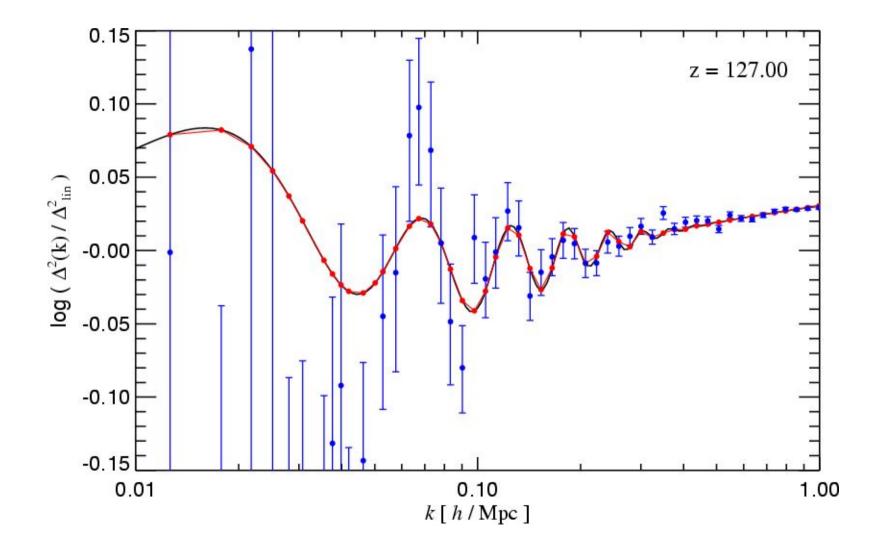
z = 3.05

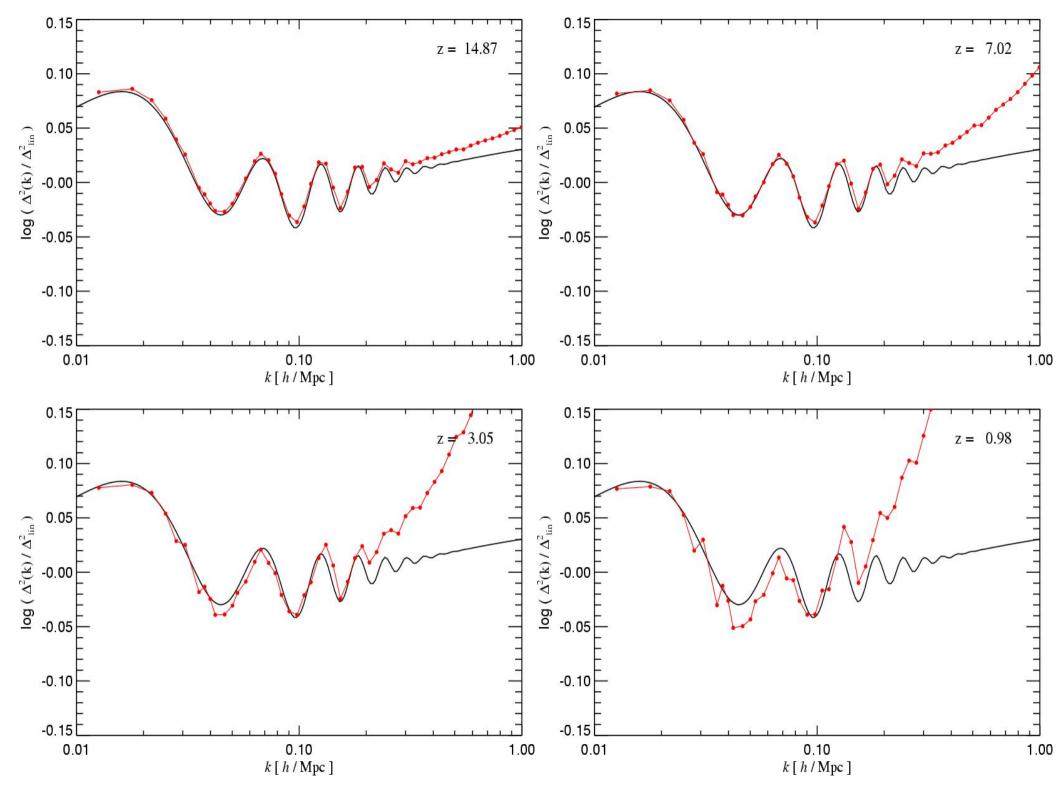
100.00

# The power in individual modes is Rayleigh distributed around the mean DISTRIBUTION OF MODE AMPLITUDES RELATIVE TO THE MEAN

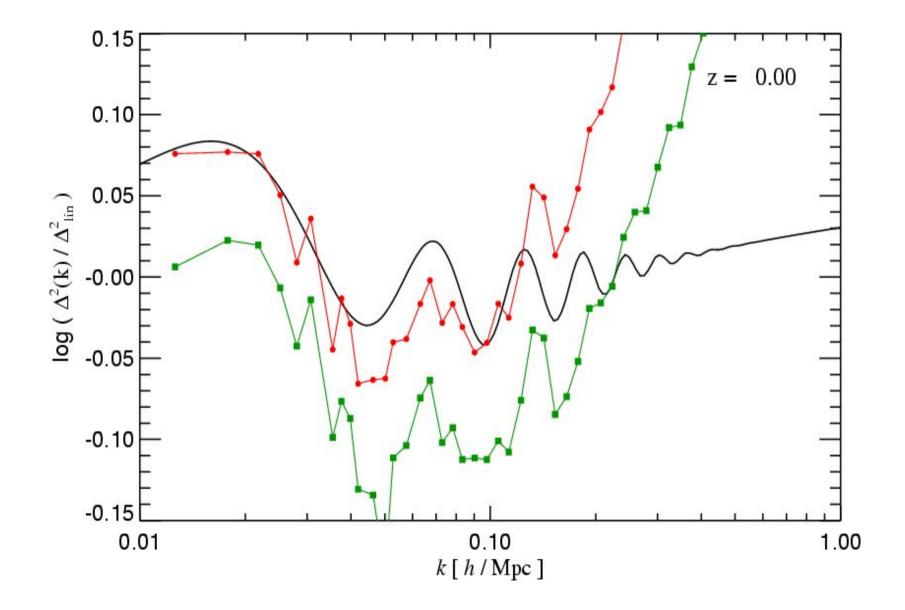


# The boxsize of the Millennium Run is large enough to resolve the baryonic wiggles in the matter power spectrum LINEAR MASS POWER SPECTRUM AT HIGH REDSHIFT

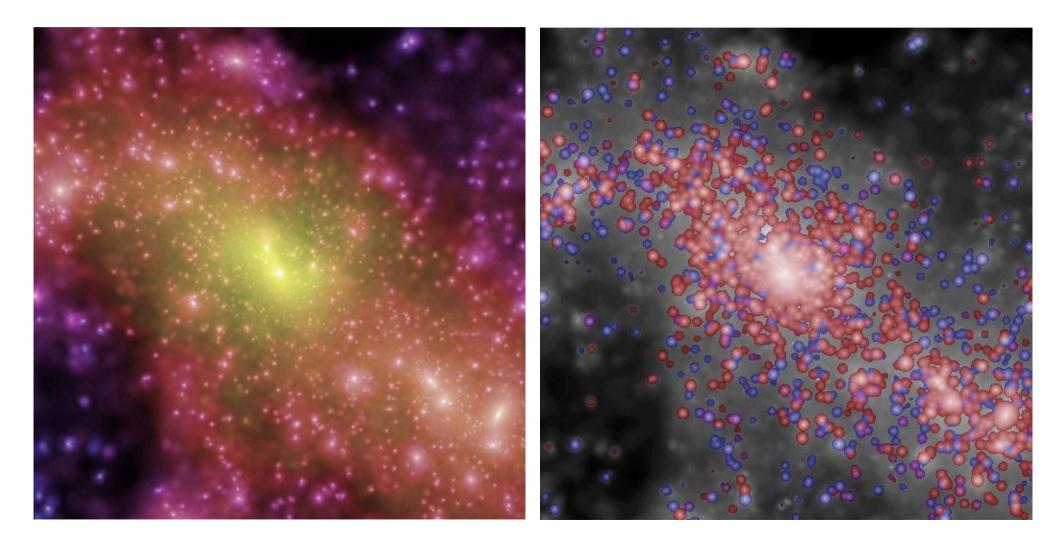




#### Non-linear evolution accelerates the growth of power and eliminates structure in the spectrum by mode-coupling LINEAR MASS POWER SPECTRUM AT THE PRESENT EPOCH

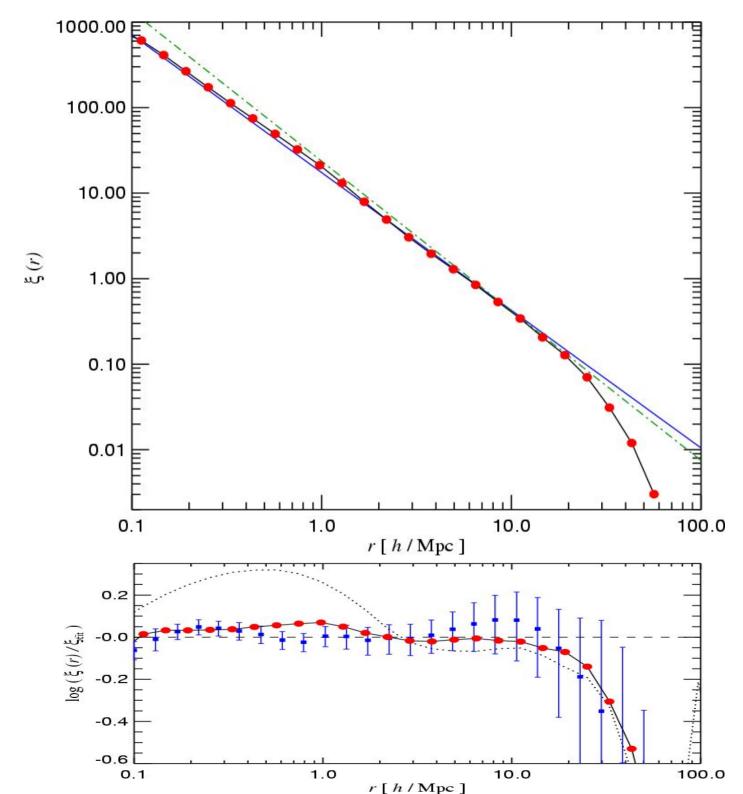


A merger tree containing 800 million dark matter (sub)halos is used to compute semi-analytic models of galaxy formation DARK MATTER AND GALAXY DISTRIBUTION IN A CLUSTER OF GALAXIES



The two-point correlation function of galaxies in the Millennium run is a very good power law

GALAXY TWO-POINT FUNCTION COMPARED WITH APM AND SDSS



#### Postprocessing of the simulation data requires effcient analysis codes VARIOUS POSTPROCESSING-TASKS

#### Things done on the fly by the simulation code

- FoF group finding
  - Power spectrum and correlation function measurement

#### Tasks carried out as true postprocessing

#### Substructure finding and halo/subhalo properties

- Done by L-SubFind in massiv parallel mode
- With 32 CPU/256 GB (chubby queue) can process one clustered snapshot in ~4-5 hours

#### Construction of merger history trees

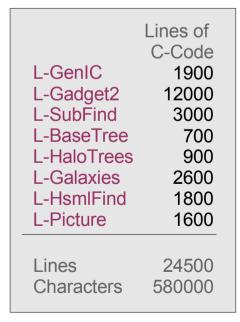
- Two step procedure. L-BaseTree finds halos descendants in future snapshots, thereby providing horizontal links in the merger tree. Serial/OpenMP-parallel, requires ~200 GB shared RAM, fast.
- In a second step, L-HaloTrees builds up fully threaded vertical trees for each halo. These are the input objects for the semi-analytic code.

#### Semi-analytic galaxy formation

- New semi-analytic code L-Galaxies, can be run in massively parallel mode on the merger trees generated for the Millennium Run.
- Interfacing with VO databases is in preparation.

#### Data visualization

Challenging because of the data volume. L-HsmlFind (massively parallel) determines dark matter adaptive smoothing lengths, while L-Picture (serial) makes a picture for an arbitrarily inclinded and arbitrarily large slice through the periodic simulation.



We recently developed a largely new cosmological code: GADGET-II NEW FEATURES OF GADGET-II

- New symplectic integration method
- Higher speed of the tree algorithm
- Less memory consumption for tree and particle storage (~100% saving)

Key feature for Millenium Run

- Code may be run optionally as a TreePM hybrid code
- SPH neighbour search faster
- Conservative SPH formulation
- Fully consistent dynamic tree updates
- Additional types of runs possible (e.g. 2D, hydrodynamics-only, long periodic boxes)
- Efficient and clean formation of star particles
- More physics
- More output options, including HDF5
- Still fully standard C & standard MPI. The FFTW and GSL libraries are needed.
- Reduced communication overhead, better scalability, arbitrary number of cpus
- Built in parallel group finder

The new code is quite a bit better than the old version...

#### Physics in GADGET-II for simulations of galaxy formation

- Radiative cooling, UV background (homogeneous)
- Subresolution multiphase model for the ISM: Star formation and feedback
- Phenomenological model for galactic winds
- Detailed chemical enrichment
- Thermal conduction
- MHD (with caveats)
- Non-thermal relativistic component (cosmic rays)
- Growth of supermassive black holes and AGN feedback

The new code is quite a bit better than the old version...

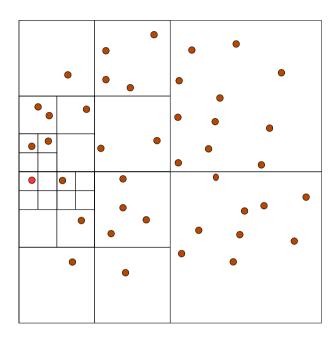
# Gravity is the driving force for structure formation in the universe HIERARCHICAL TREE ALGORITHMS

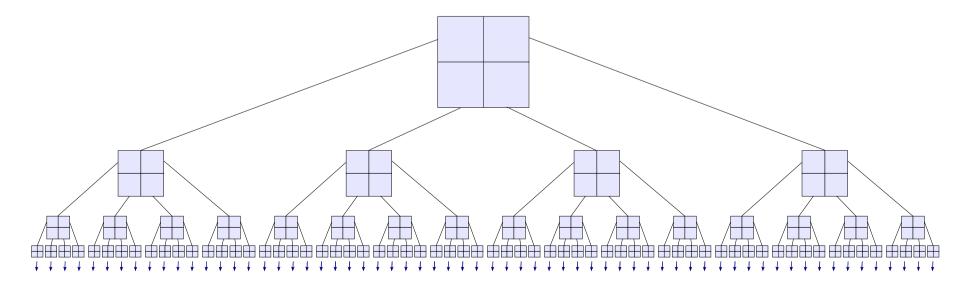
The N<sup>2</sup> - scaling of direct summation puts serious limitations on N...

But we want N ~  $10^{6}$ - $10^{10}$  for collisionless dynamics of dark matter !

**Idea:** Group distant particles together, and use their multipole expansion.

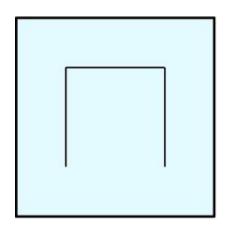
 $\rightarrow$  Only  $\sim$  log(N) force terms per particle.

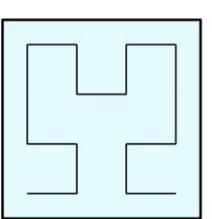


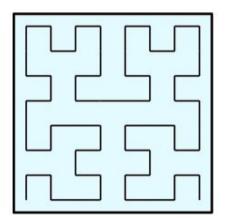


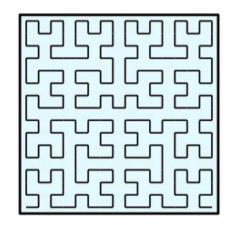
The tree-algorithm of Gadget-2 has been optimized for providing better memory locality REDUCTION OF CACHE MISSES AND DOMAIN DECOMPOSITION Idea: Order the particles along a space-filling curve

Hilbert's curve: A fractal that fills the square

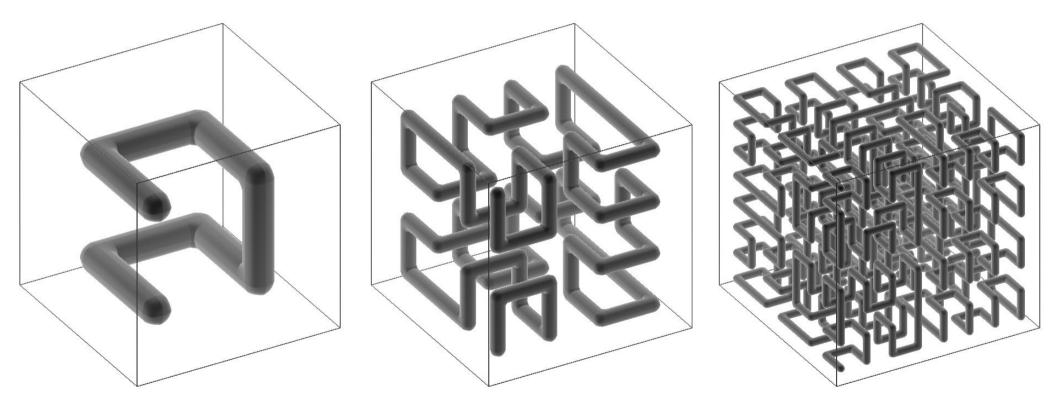






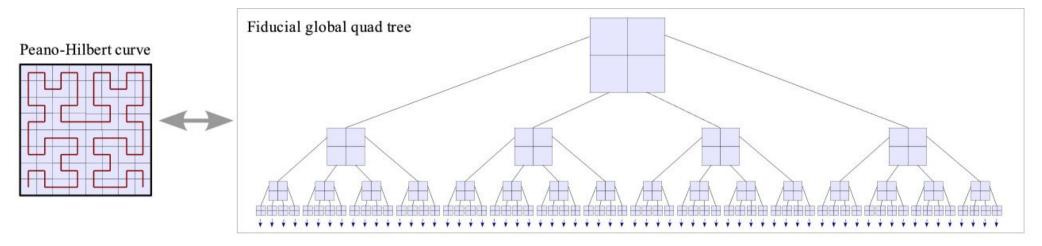


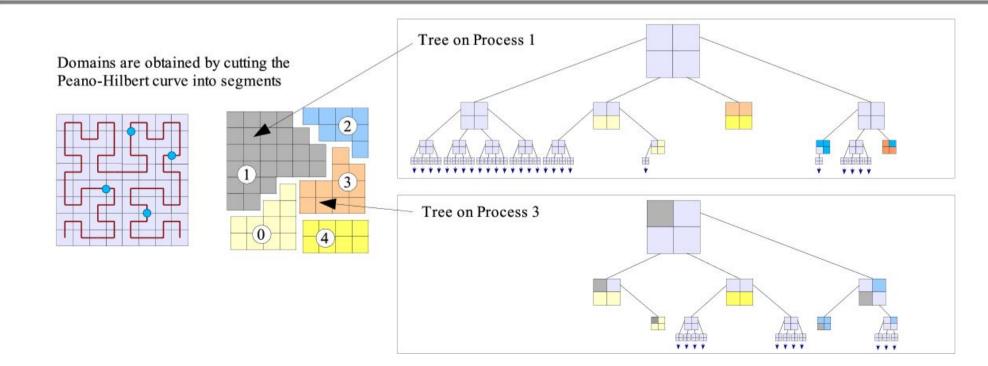
### The space-filling Hilbert curve can be readily generalized to 3D THE PEANO-HILBERT CURVE



### A space-filling Peano-Hilbert curve is used in GADGET-2 for a novel domain-decomposition concept

#### HIERARCHICAL TREE ALGORITHMS





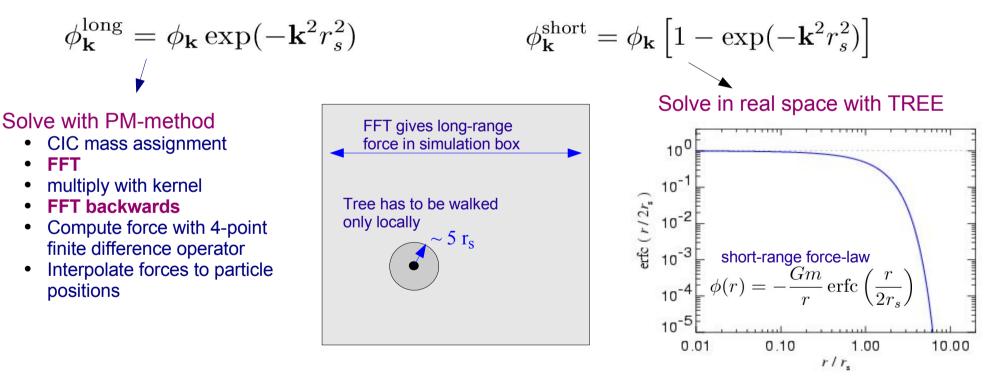
# The TreePM technique combines the advantages of PM-method and Tree-algorithm

#### THE TREE-PM FORCE SPLIT

Periodic peculiar potential 
$$\nabla^2 \phi(\mathbf{x}) = 4\pi G[\rho(\mathbf{x}) - \overline{\rho}] = 4\pi G \sum_{\mathbf{n}} \sum_i m_i \left[ \tilde{\delta}(\mathbf{x} - \mathbf{x}_i - \mathbf{n}L) - \frac{1}{L^3} \right]$$

**Idea:** Compute the long-range force with the PM algorithm, and only a **local** short-range force with the tree.

Let's split the potential in Fourier space into a long-range and a short-range part:



Advantages of this algorithm include:

- Accurate and fast long-range force
- No force anisotropy
- Speed is insensitive to clustering (as for tree algorithm)
- No Ewald correction necessary for periodic boundary conditions

#### Symplectic integration schemes can be generated by applying the idea of operating splitting to the Hamiltonian THE LEAPFROG AS A SYMPLECTIC INTEGRATOR

Separable Hamiltonian

$$H = H_{\rm kin} + H_{\rm pot}$$

**Drift- and Kick-Operators** 

$$\mathbf{D}(\Delta t) \equiv \exp\left(\int_{t}^{t+\Delta t} \mathrm{d}t \,\mathbf{H}_{\mathrm{kin}}\right) = \begin{cases} \mathbf{p}_{i} & \mapsto & \mathbf{p}_{i} \\ \mathbf{x}_{i} & \mapsto & \mathbf{x}_{i} + \frac{\mathbf{p}_{i}}{m_{i}}\Delta t \end{cases}$$
$$\mathbf{K}(\Delta t) = \exp\left(\int_{t}^{t+\Delta t} \mathrm{d}t \,\mathbf{H}_{\mathrm{pot}}\right) = \begin{cases} \mathbf{x}_{i} & \mapsto & \mathbf{x}_{i} \\ \mathbf{p}_{i} & \mapsto & \mathbf{p}_{i} - \sum_{j} m_{i} m_{j} \frac{\partial \phi(\mathbf{x}_{ij})}{\partial \mathbf{x}_{i}}\Delta t \end{cases}$$

1 1 1

The drift and kick operators are symplectic transformations of phase-space !

The Leapfrog

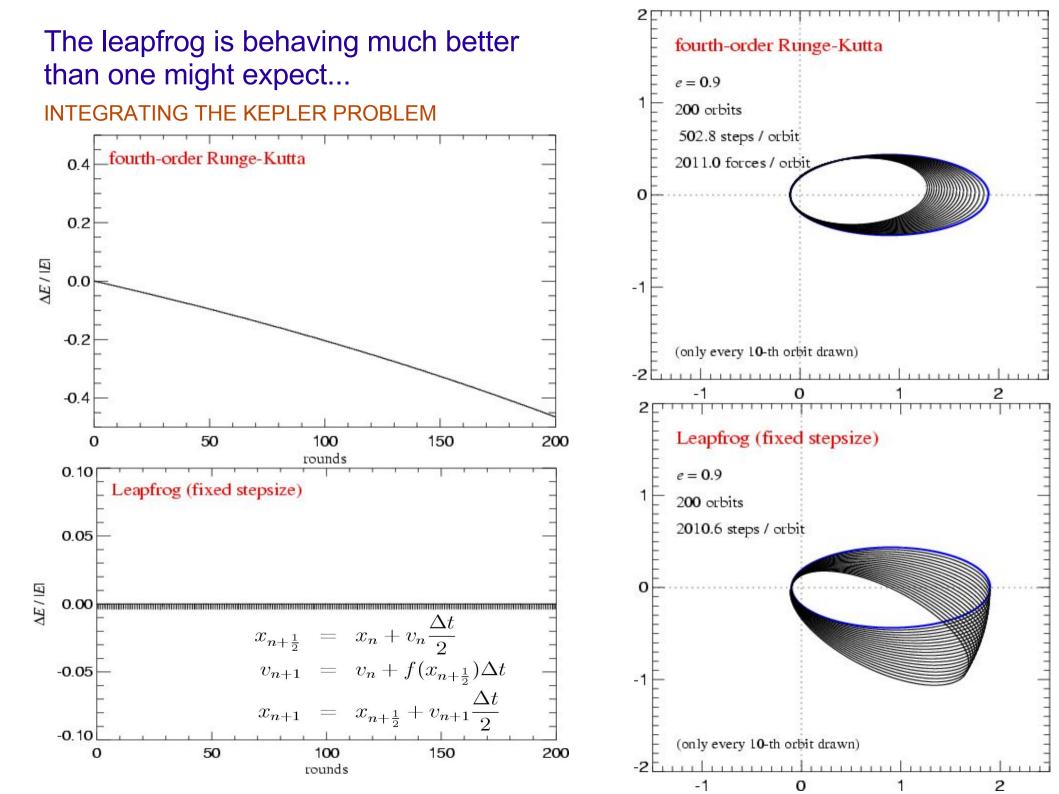
Drift-Kick-Drift:

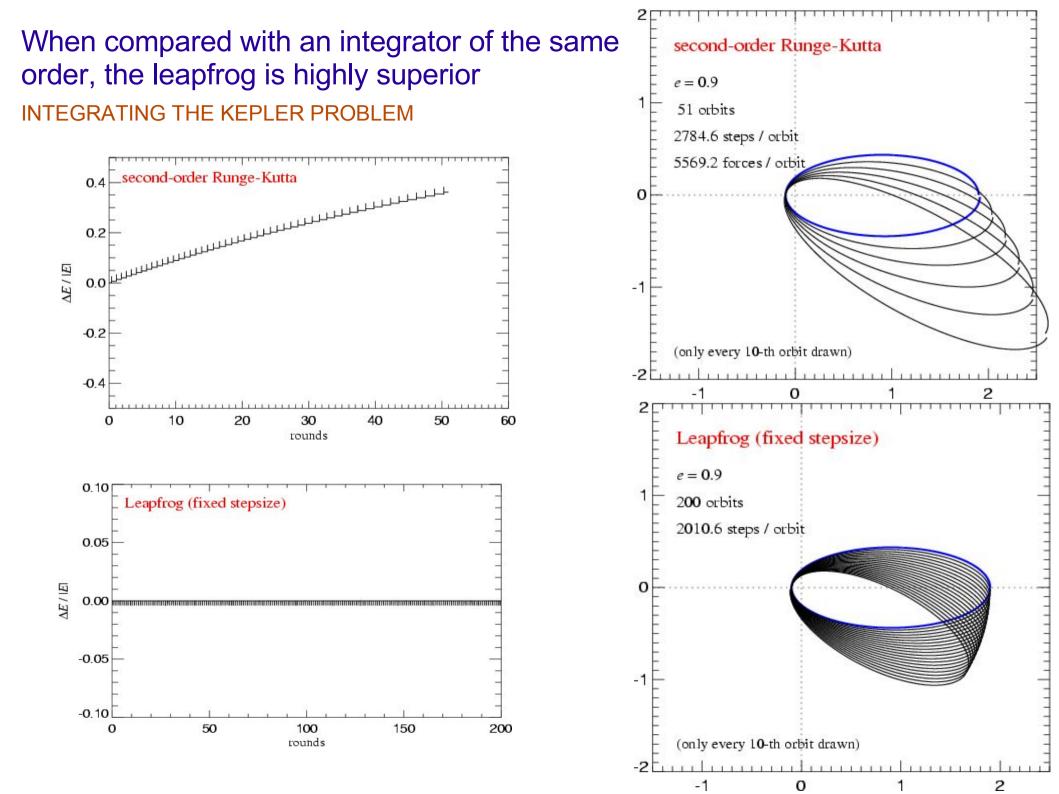
$$\tilde{\mathbf{U}}(\Delta t) = \mathbf{D}\left(\frac{\Delta t}{2}\right) \,\mathbf{K}(\Delta t) \,\mathbf{D}\left(\frac{\Delta t}{2}\right)$$
$$\tilde{\mathbf{U}}(\Delta t) = \mathbf{K}\left(\frac{\Delta t}{2}\right) \,\mathbf{D}(\Delta t) \,\mathbf{K}\left(\frac{\Delta t}{2}\right)$$

/ A / N

Hamiltonian of the numerical system:

$$\tilde{H} = H + H_{\text{err}} \qquad H_{\text{err}} = \frac{\Delta t^2}{12} \left\{ \left\{ H_{\text{kin}}, H_{\text{pot}} \right\}, H_{\text{kin}} + \frac{1}{2} H_{\text{pot}} \right\} + \mathcal{O}(\Delta t^3)$$





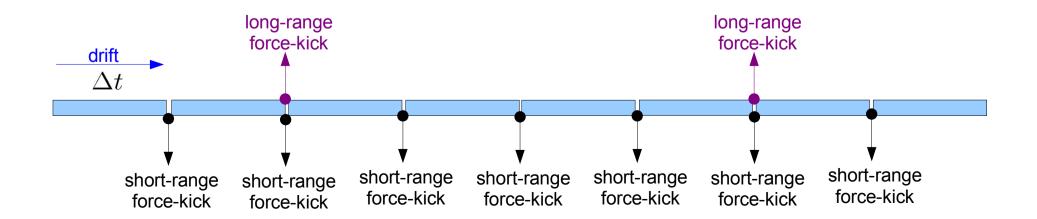
The force-split can be used to construct a symplectic integrator where long- and short-range forces are treated independently TIME INTEGRATION FOR LONG AND SHORT-RANGE FORCES

Separate the potential into a long-range and a short-range part:

$$H = \sum_{i} \frac{\mathbf{p}_i^2}{2m_i a(t)^2} + \frac{1}{2} \sum_{ij} \frac{m_i m_j \varphi_{\rm sr}(\mathbf{x}_i - \mathbf{x}_j)}{a(t)} + \frac{1}{2} \sum_{ij} \frac{m_i m_j \varphi_{\rm lr}(\mathbf{x}_j - \mathbf{x}_j)}{a(t)}$$

The short-range force can then be evolved in a symplectic way on a smaller timestep than the long range force:

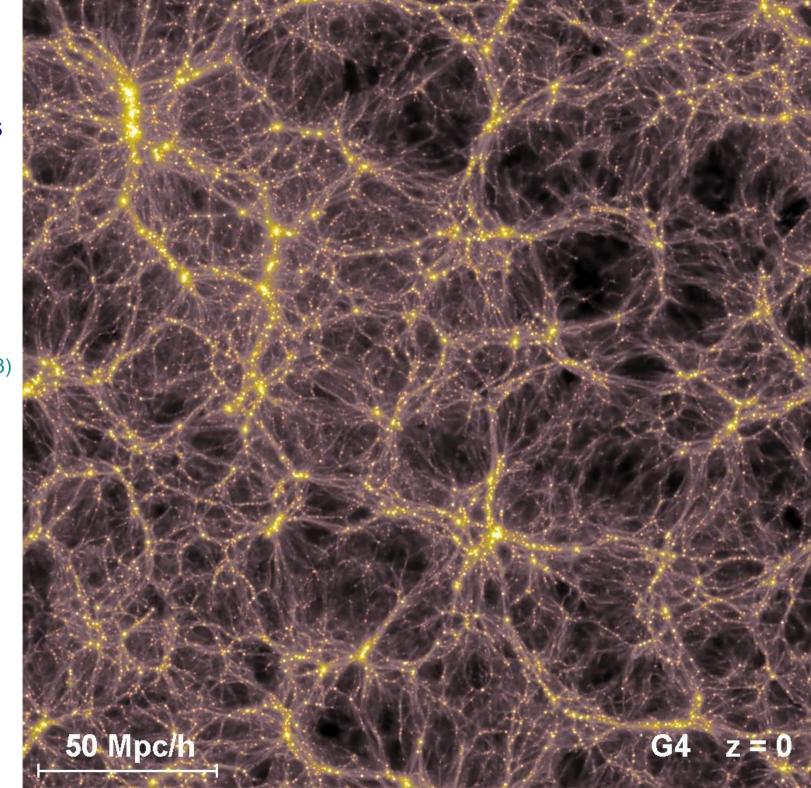
$$\tilde{\mathbf{U}}(\Delta t) = \mathbf{K}_{\mathrm{lr}}\left(\frac{\Delta t}{2}\right) \left[\mathbf{K}_{\mathrm{sr}}\left(\frac{\Delta t}{2m}\right) \mathbf{D}\left(\frac{\Delta t}{m}\right) \mathbf{K}_{\mathrm{sr}}\left(\frac{\Delta t}{2m}\right)\right]^{m} \mathbf{K}_{\mathrm{lr}}\left(\frac{\Delta t}{2}\right)$$



A faithful representation of cosmic structure formation requires large simulation volumes

BARYONIC DENSITY IN SIMULATIONS WITH RADIATIVE COOLING, STAR FORMATION AND FEEDBACK

Springel & Hernquist (2003)



#### Modeling a true multi-phase ISM in cosmological volumes is currently not feasible

THE COMPUTATIONAL CHALLENGE

#### Giant molecular clouds

 $\begin{array}{lll} M_{\rm cl} & \sim & 5 \times 10^5 \,\, {\rm M}_\odot & & {\rm for} \,\, L \\ R_{\rm cl} & \sim & 30 \,\, {\rm pc} & & \\ \overline{n} & \sim & 200 \,\, {\rm cm}^{-3} & & M_{\rm sph} \\ \delta & \sim & 10^9 & & \epsilon \\ t_{\rm cl} & \sim & 4 \times 10^6 \,\, {\rm yr} & & \delta \end{array}$ 

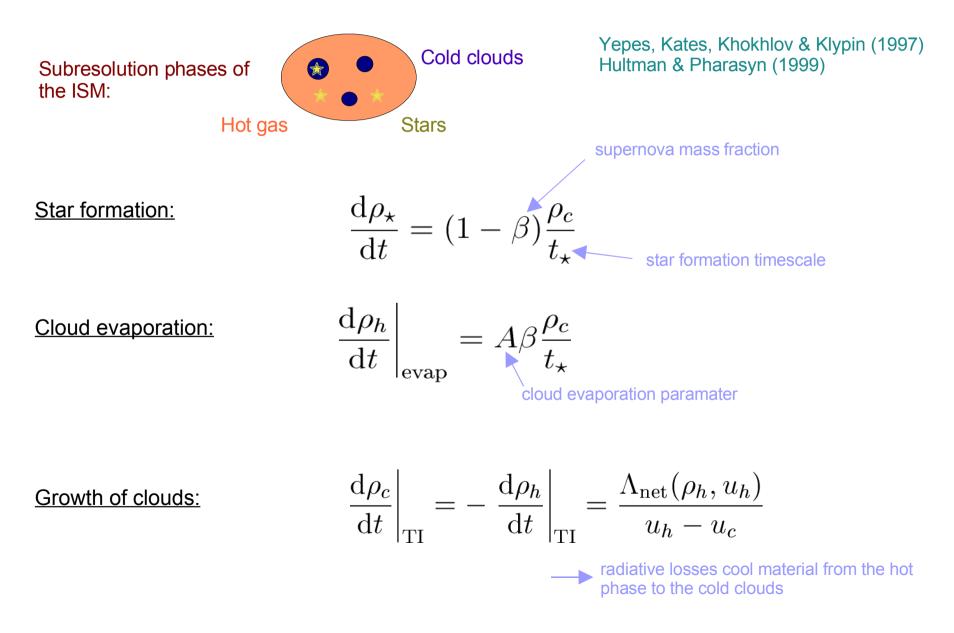
 $\begin{array}{l} \hline \mbox{Currently achievable resolution} \\ \mbox{for } L \geq 50 \ h^{-1} \mbox{Mpc:} \\ \\ M_{\rm sph} \sim 10^7 \ \mbox{M}_{\odot} \\ \\ \epsilon \sim 1 \ \mbox{kpc} \\ \\ \delta \sim 10^7 \end{array}$ 

huge dynamic range + difficult/unclear physics !

Need to develop effective subgrid-models that are motivated by physical models of the ISM

### A simple multi-phase model for cosmological simulations

#### MODEL EQUATIONS



Thermal energy budget:

supernova `temperature' ~ 108 K

1

$$\frac{\mathrm{d}}{\mathrm{d}t} \left( \rho_h u_h + \rho_c u_c \right) = -\Lambda_{\mathrm{net}}(\rho_h, u_h) + \beta \frac{\rho_c}{t_\star} u_{\mathrm{SN}} - (1 - \beta) \frac{\rho_c}{t_\star} u_c,$$
Total energy Cooling Feedback Loss to stars

cold clouds:

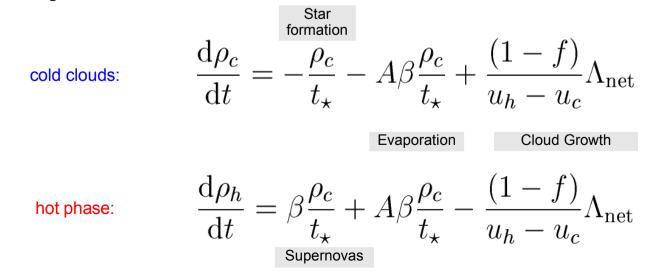
$$\frac{\mathrm{d}}{\mathrm{d}t}\left(\rho_{c}u_{c}\right) = -\frac{\rho_{c}}{t_{\star}}u_{c} - A\beta\frac{\rho_{c}}{t_{\star}}u_{c} + \frac{(1-f)u_{c}}{u_{h} - u_{c}}\Lambda_{\mathrm{net}}$$

$$f = \begin{cases} 1 & \text{normal cooling} \\ 0 & \text{thermal instability} \end{cases}$$

hot phase:

$$\frac{\mathrm{d}}{\mathrm{d}t}\left(\rho_{h}u_{h}\right) = \beta \frac{\rho_{c}}{t_{\star}}(u_{\mathrm{SN}} + u_{c}) + A\beta \frac{\rho_{c}}{t_{\star}}u_{c} - \frac{u_{h} - fu_{c}}{u_{h} - u_{c}}\Lambda_{\mathrm{net}}$$

Mass transfer budget:



#### Temperature evolution:

hot phase:  $\rho_h \frac{\mathrm{d}u_h}{\mathrm{d}t} = \left[ u_{\mathrm{SN}} - (A+1)(u_h - u_c) \right] \beta \frac{\rho_c}{t_\star} - f\Lambda_{\mathrm{net}}$ cold clouds: temperature assumed to be constant at ~ 10<sup>4</sup> K equilibirum temperature for star formation
+ thermal instability  $u_h = \frac{u_{\mathrm{SN}}}{A+1} + u_c$ 

**Evaporation efficiency:** 

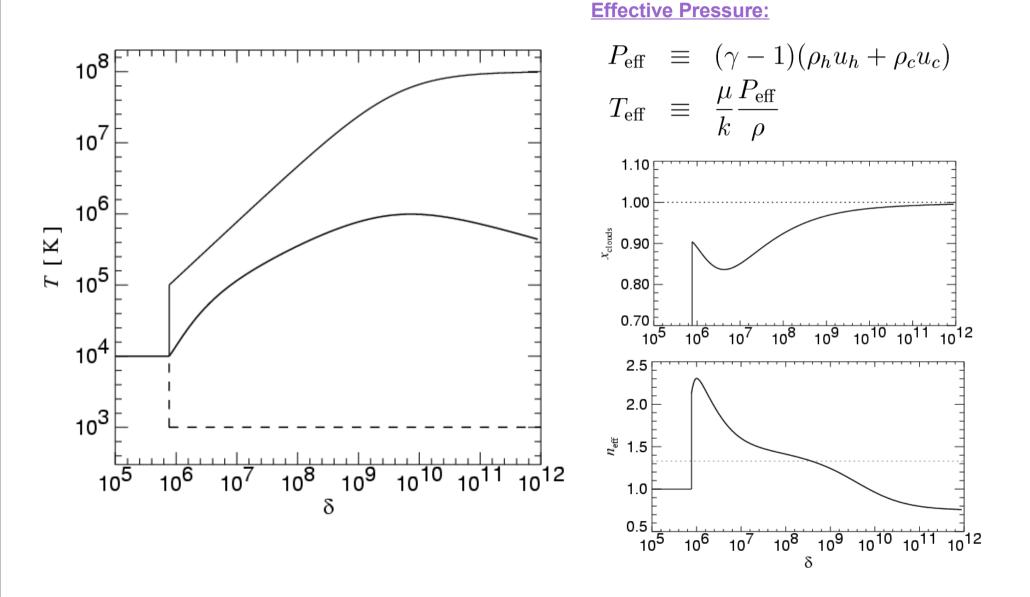
$$A(\rho) = A_0 \left(\frac{\rho}{\rho_{\rm th}}\right)^{-4/5}$$

Star formation timescale:

$$t_{\star}(\rho) = t_{\star}^{0} \left(\frac{\rho}{\rho_{\rm th}}\right)^{-1/2}$$

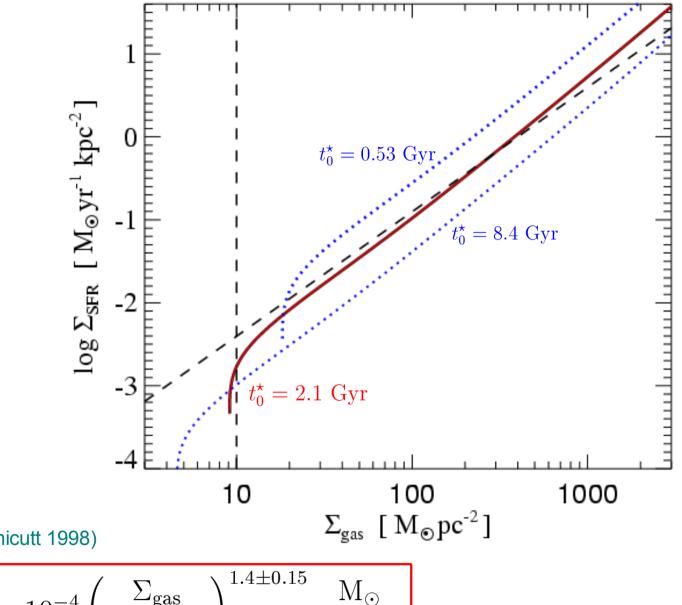
 $\rho_{\rm th} \text{ and } A_0 \text{ are constraint by} \longrightarrow \text{ star formation timescale } t_{\star}^0$ plausible temperature range of the ISM is adjustable parameter of model

### The ISM is pressurized by star formation in the region of coexistence between a hot medium and embedded cold clouds EFFECTIVE EQUATION OF STATE



# Self-gravitating sheets of gas are used to normalize the multi-phase model

KENNICUTT LAW

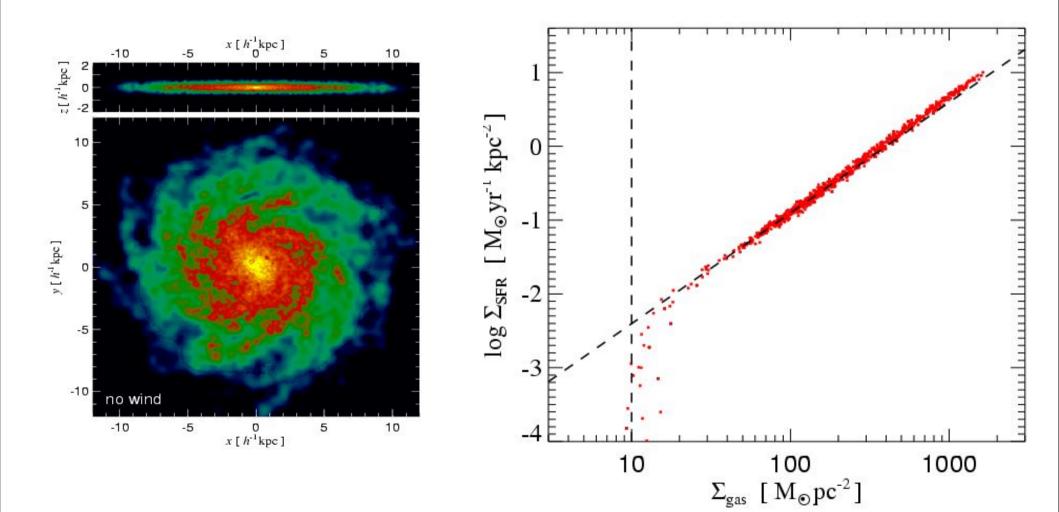


Global "Kennicutt-law" (Kennicutt 1998)

$$\Sigma_{\rm SFR} = (2.5 \pm 0.7) \times 10^{-4} \left(\frac{\Sigma_{\rm gas}}{M_{\odot} {\rm pc}^{-2}}\right)^{1.4 \pm 0.15} \frac{{\rm M}_{\odot}}{{\rm yr \, kpc}^2}$$

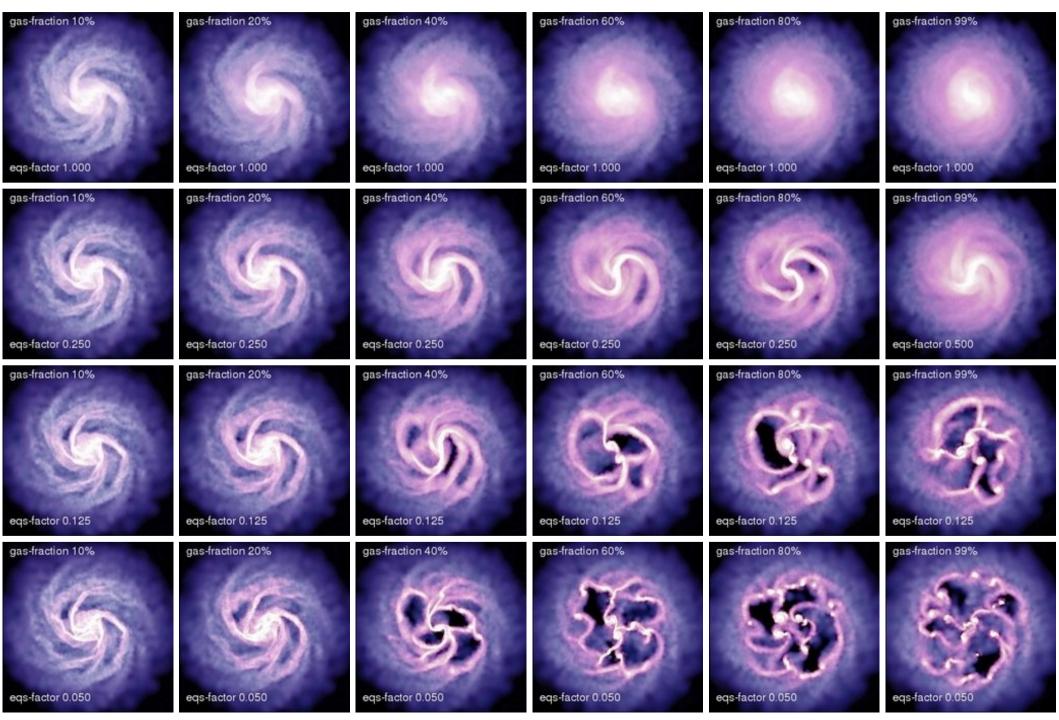
## Simulations of isolated disk galaxies are used to check the normalization of the multi-phase model

MEASURED KENNICUTT LAW



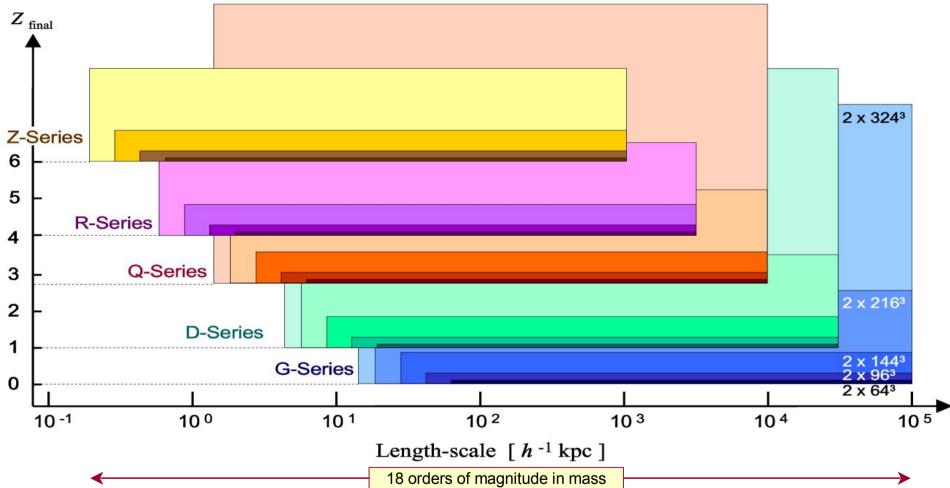
#### The multiphase-model allows stable disk galaxies even for very high gas surface densities

STABILITY OF DISKS AS A FUNCTION OF GAS FRACTION AND EQUATION OF STATE



### We have run a program of simulations on a set of interlocking scales and resolutions

### SIMULATION PROGRAM





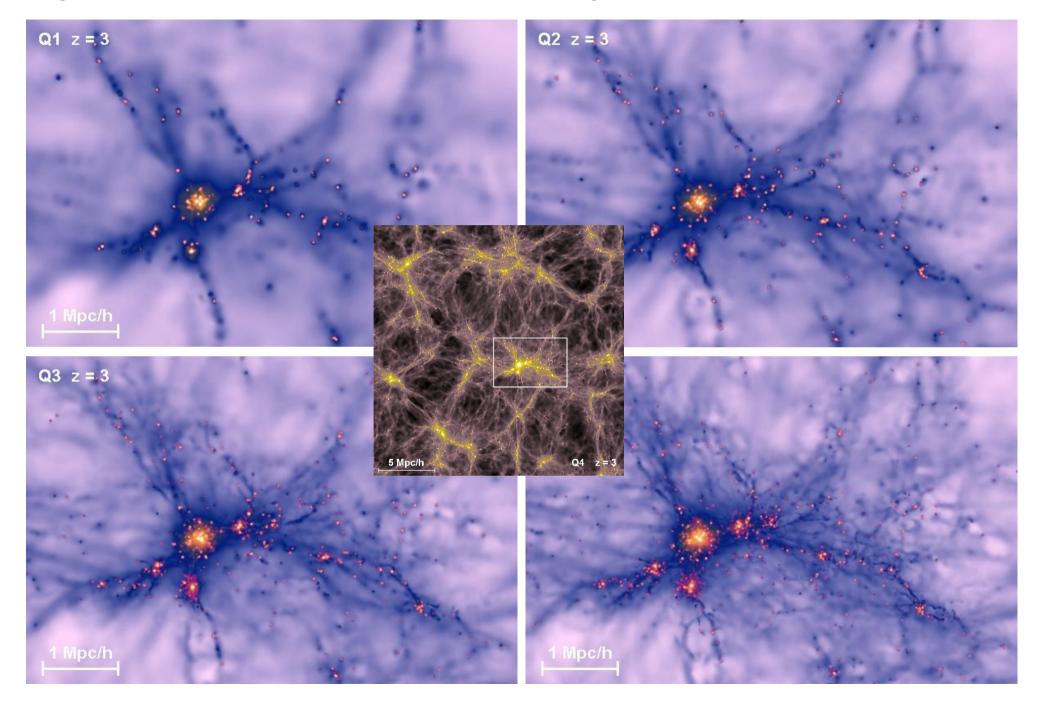
Run on Mako, Harvard - CfA

#### **Beowulf-class computer**

**Configuration:** 

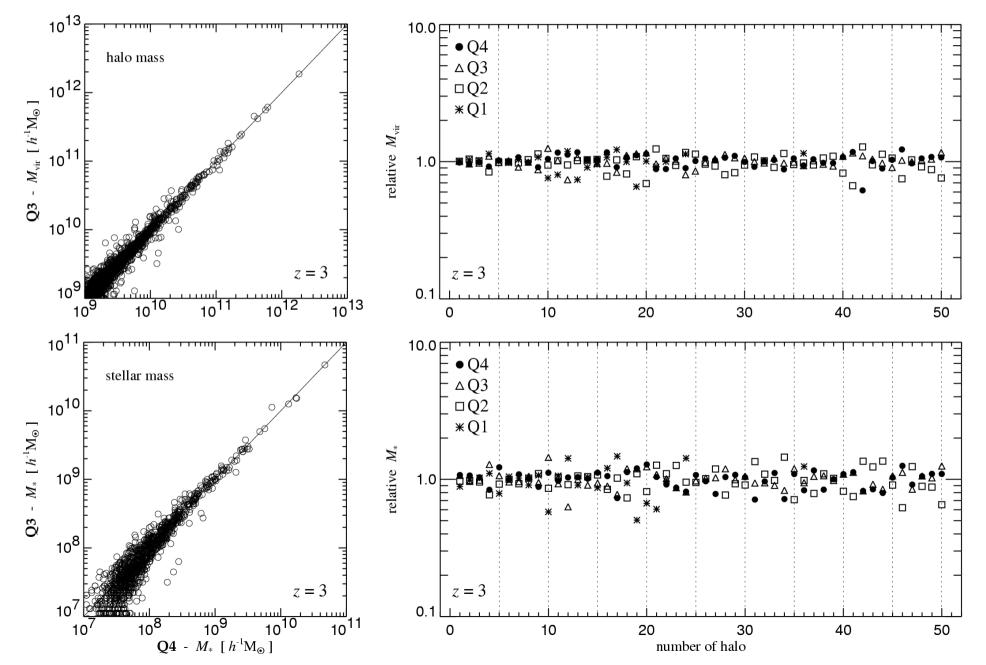
256 Athlon MP (1.6 GHz) arranged in 128 double-processor SMP nodes with 1 GB RAM each, 100 Base-T switched Ethernet, Linux Separate Frontend and 2 big Fileservers

## Higher mass resolution can resolve smaller galaxies



## The star formation rate of individual galaxies converges well for sufficient mass resolution

**OBJECT-BY-OBJECT RESOLUTION STUDY** 

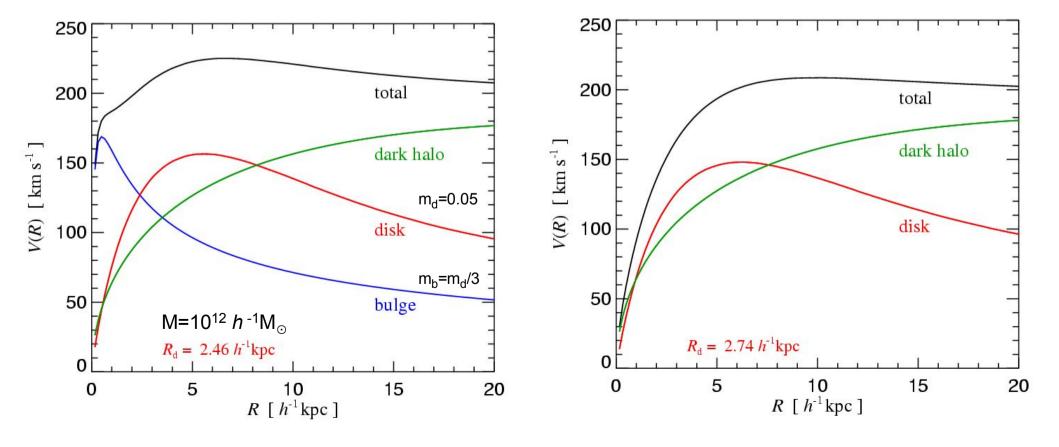


## We construct compound disk galaxies that are in dynamical equilibrium

STRUCTURAL PROPERTIES OF MODEL GALAXIES

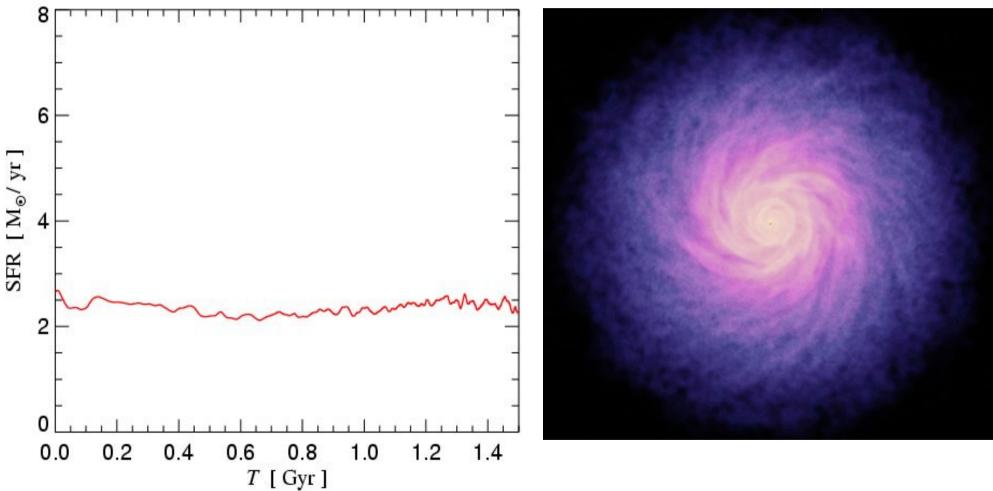
#### **Components:**

- Dark halo (Hernquist profile matched to NFW halo)
- Stellar disk (expontial)
- Stellar bulge
- Gaseous disk (expontial)
- Central supermassive black hole (small seed mass)
- We compute the exact gravitational potential for the axisymmetric mass distribution and solve the Jeans equations
- Gas pressure effects are included
- The gaseous scale-height is allowed to vary with radius



## Carefully constructed compound galaxies are stable when evolved in isolation

TIME EVOLUTION OF AN ISOLATED GALAXY WITH A CENTRAL BLACK HOLE

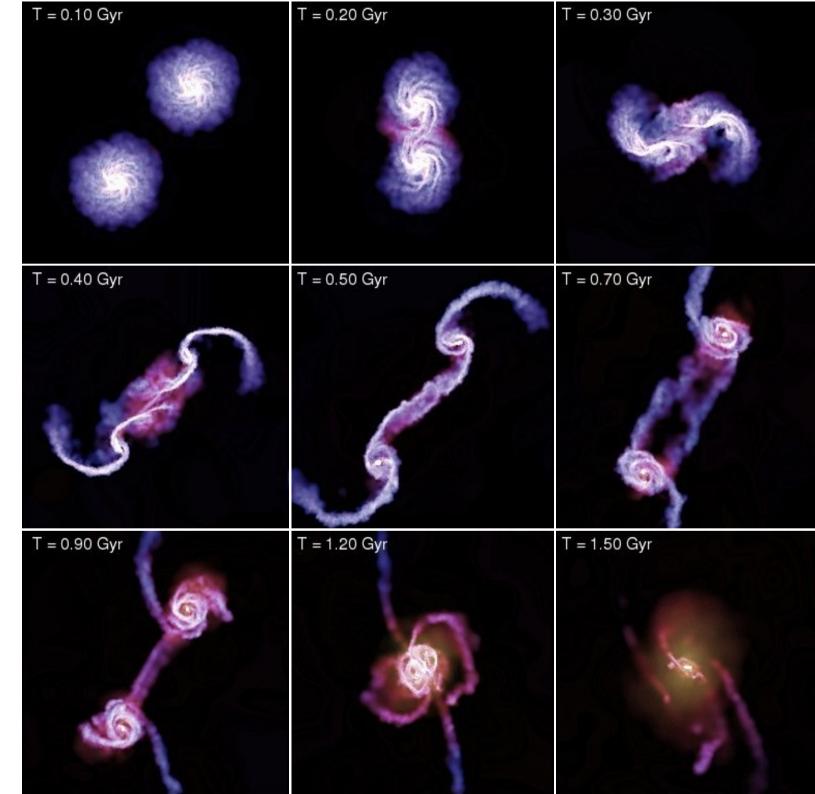


star formation rate

In major-mergers between two disk galaxies, tidal torques extract angular momentum from cold gas, providing fuel for nuclear starbursts

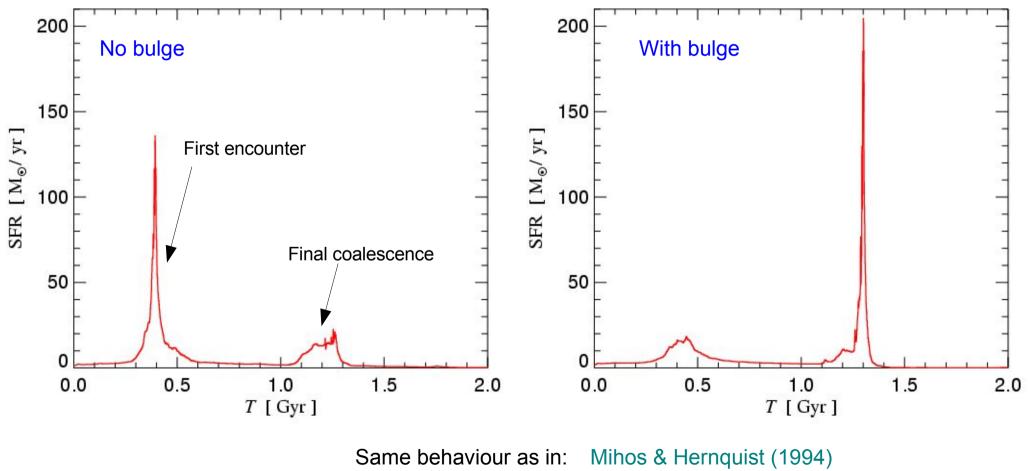
TIME EVOLUTION OF A PROGRADE MAJOR MERGER

This may also fuel a central AGN !



# The strength and morphology of the starburts depends on the structural stability of the disks, and on the collision orbit

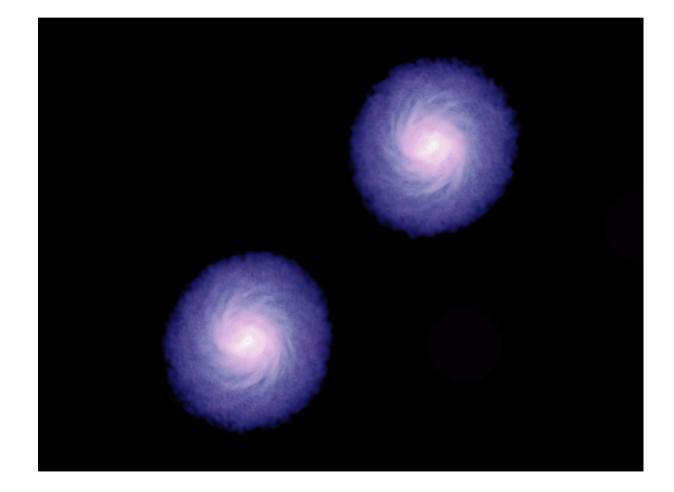
STARBURSTS IN MODELS WITH ISOTHERMAL EQUATION OF STATE



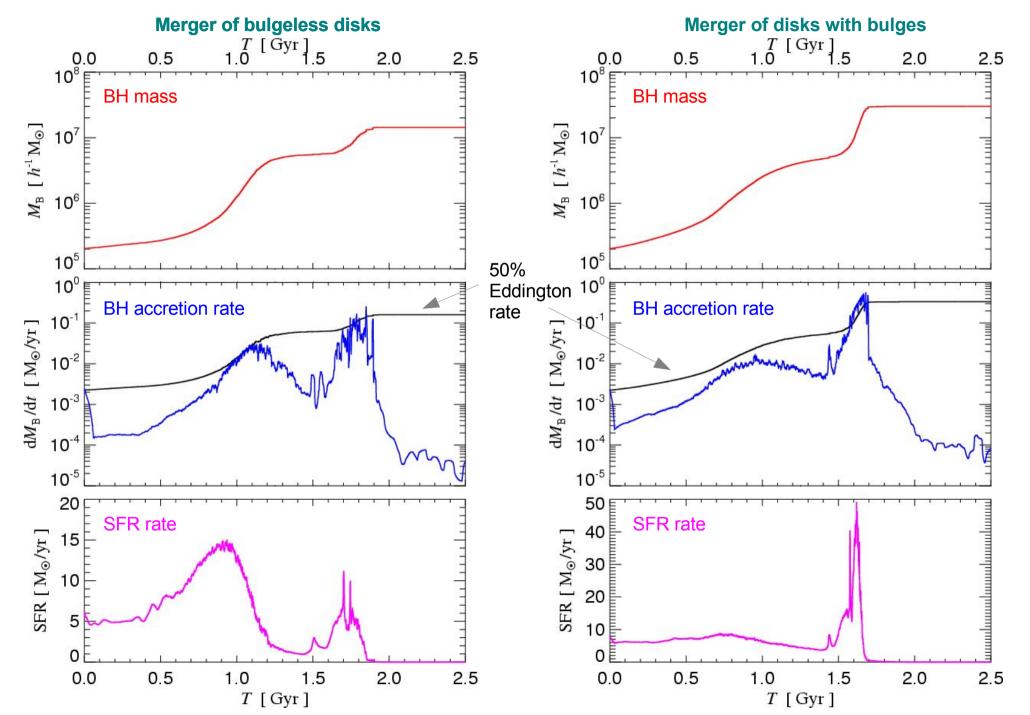
Springel (2000)

In mergers with supermassive black holes, simultaneous feeding of nuclear starbursts and central AGN activity occurs TIME EVOLUTION OF A MERGER WITH CENTRAL BLACK HOLE ACCRETION

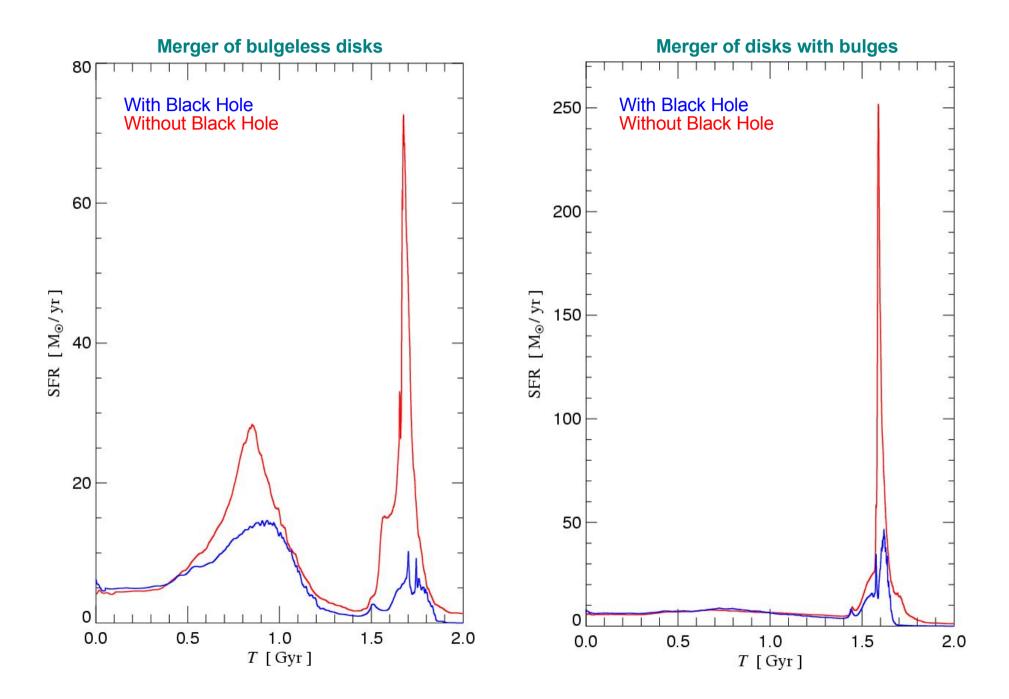
The movie...



## Mergers of disk galaxies trigger starburts and ignite central AGN activity TIME EVOLUTION OF STAR FORMATION RATE AND BLACK HOLE GROWTH IN A MERGER



## The feedback by the AGN can reduce the strength of the starburst COMPARISON OF STAR FORMATION IN MERGERS WITH AND WITHOUT BLACK HOLE

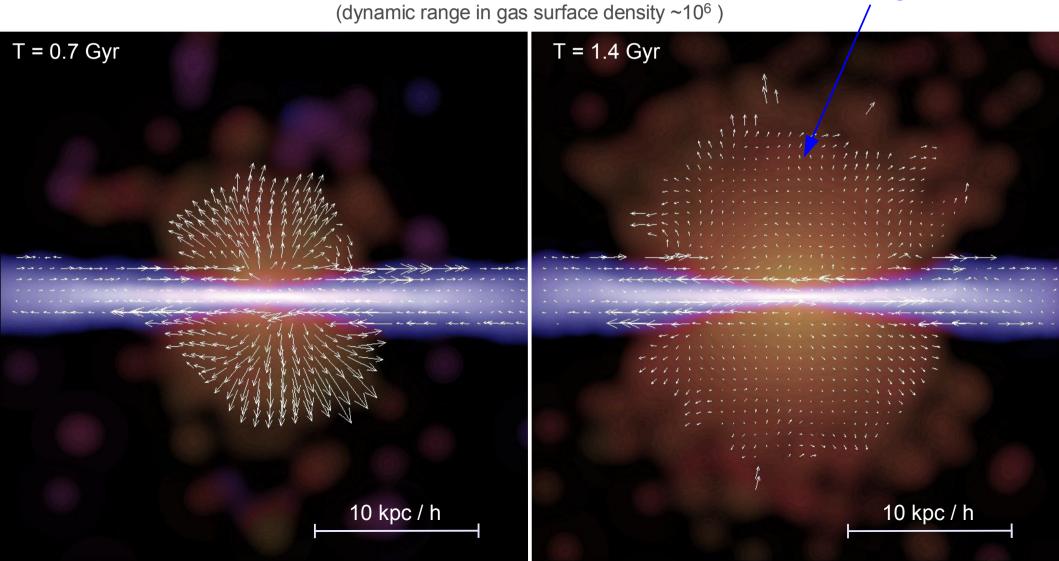


### At low accretion rates, feedback by the central black hole activity may blow a weak wind into the halo

GAS FLOW INTO THE HALO

Isolated disk galaxy with bulge

Generated hot halos holds 1-2% of the gas



# The feedback by the central black activity may drive a strong quasar windGAS OUTFLOW BY AGN FEEDBACK(outflow reaches speeds of up to ~1800 km/sec)

T = 0.5 Gyr/h T = 0.4 Gyr/h 30 kpc / h 0 9 Avr

The properties of merger remnants are altered by the AGN activity THE FATE OF THE GAS IN A MERGER WITH AND WITHOUT BLACK HOLES

#### Merger without black hole:

initial gas mass: 1.56 x  $10^{10} h^{-1} M_{\odot}$ 

- 89.0% turned into stars
- 0.05% expelled from halo
- 1.2% cold, star forming gas
- 9.8% diffuse gas in halo

### X-ray luminosity

~ 9.5 x 10<sup>39</sup> erg s<sup>-1</sup>

#### Residual star formation rate

 $\sim 0.13 \ {\rm M}_{\odot} {\rm yr}^{-1}$ 

(1 Gyr after galaxy coalesence)

#### Merger with black hole:

initial gas mass: 1.56 x  $10^{10} h^{-1} M_{\odot}$ 

- 51.9% turned into stars
- 35.3% expelled from halo
- 0% cold, star forming gas
- 11.1% diffuse gas in halo
- 1.6% swallowed by BH(s)
- X-ray luminosity

~ 4.8 x 10<sup>38</sup> erg s<sup>-1</sup>

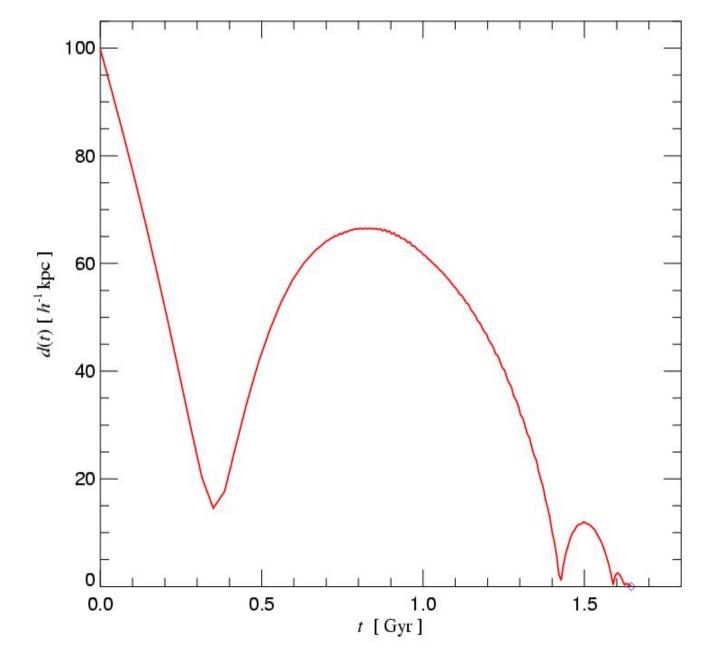
Residual star formation rate

 $0~M_{\odot}yr^{-1}$ 

(1 Gyr after galaxy coalesence)

## Galaxy mergers bring their central supermassive black holes quickly to separations less than ~100 pc

APPROACH OF THE BLACK HOLES IN MERGER SIMULATIONS



Note: The actual formation of a black hole binary, and the hardening of it, cannot presently be addressed by our simulations in an adequate way, due to lack of spatial dynamic range.

### Conclusions

- We have implemented new numerical methods which allow us to carry out unprecedently large, high-resolution cosmological N-body simulations. We achieve N>10<sup>10</sup>, with a formal dynamic range of 10<sup>5</sup> in 3D.
- A suite of advanced analysis software has been developed. It will allow the construction of theoretical mock galaxy catalogues, describing the history of 25 million galaxies. This will form one of the backbones of an emerging *Theoretical Virtual Observatory*.
- We have implemented new numerical methods which allow us to carry out large, high-resolution cosmological simulations of galaxy formation that track the growth of galactic supermassive black holes. The growth of black holes is self-regulated by AGN feedback.
- Mergers of galaxies exhibit a complex interplay between starbursts and nuclear AGN activity. In a major merger, star formation and accretion can be terminated on very short timescales, with the black hole driving a strong quasar outflow. As a result, the merger left behind is a comparatively gas-poor, "dead" elliptical, which quickly develops a red stellar color.