0.0 Gyr

Stars 0.1 Gyr

Stars

10 kpc

Milky Way

10 kpc

Starburst Disks

The Structure of the Interstellar Medium: Turbulence, Gravity, & Feedback

0.1 Gyr

Stars

Gas 0.1 Gyr 10 kpc

10 kpc

Philip Hopkins

with Eliot Quataert, Norm Murray, Lars Hernquist, Dusan Keres, Todd Thompson, Desika Narayanan, Dan Kasen, T. J. Cox, Chris Hayward, Kevin Bundy, & more

The Structure of the Interstellar Medium: Turbulence, Gravity, & Feedback

0.1 Gyr



0.1 Gyr

10 kpc

Philip Hopkins

10 kpc

PFH 2011, 2012 (arXiv:1111.2863, 1201.4387) PFH, Quataert, & Murray 2011a,b,c (arXiv: 1101.4940, 1110.4636, 1110.4638)

Stars



Overview

> (1) The Problem

> (2) The ISM as a Random Process:

Supersonic Turbulence + Gravity: Regularity from Chaos

Applications of the "Excursion Set" Formalism

(3) What Role Does "Feedback" Physics Play? "Microphysics" of the ISM





The ISM SUPER-SONIC TURBULENCE DOMINATES (ALMOST) ALL SCALES





- **Gravity**
- Turbulence
- Magnetic, Thermal, Cosmic Ray, Radiation Pressure
- Cooling (atomic, molecular, metal-line, free-free)
- Star & BH Formation/Growth
- "Feedback": Massive stars, SNe, BHs, external galaxies, etc.

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The ISM YET THERE IS SURPRISING REGULARITY



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$$E(k) \propto k^{-p} \qquad dE \equiv E(k) dk$$
$$(k E(k) \sim u_t(k)^2)$$

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$$dp(\ln \rho | R) = \frac{1}{\sqrt{2\pi S(R)}} \exp\left[\frac{-(\ln \rho - \langle \ln \rho \rangle)^2}{2 S(R)}\right]$$



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$$S_k = \ln\left[1 + \alpha \mathcal{M}(k)^2\right]$$

$$Lemaster & Stone 2009$$

$$1 \qquad 2 \qquad 3$$

$$\ln(1 + 0.5 \text{ Mach}^2)$$

$$S(R) = \int d\ln k S_k |W(k, R)|^2$$

Extended Press-Schechter / Excursion-Set Formalism

- Press & Schechter '74:
 - r Fluctuations a Gaussian random field
 - Know linear power spectrum P(k~1/r): variance ~ k³ P(k)





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 Generalize to conditional probabilities,
 N-point statistics, resolve "cloud in cloud" problem (e.g. Bond et al. 1991)





$$\omega^2 = \kappa^2 + c_s^2 k^2 + u_t(k)^2 k^2 - \frac{4\pi G \rho |k|h}{1 + |k|h}$$

Chandrasekhar '51, Vandervoort '70, Toomre '77

$$\omega^2 = \kappa^2 + c_s^2 \, k^2 + u_t(k)^2 \, k^2 - \frac{4\pi \, G \, \rho \, |k| h}{1 + |k| h}$$
 Angular Momentum

 $\kappa \sim \frac{V_{\rm disk}}{R_{\rm disk}}$

Chandrasekhar '51, Vandervoort '70, Toomre '77



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Chandrasekhar '51, Vandervoort '70, Toomre '77



Mode Grows (Collapses) when w<0:

$$\rho > \rho_c(k) = \rho_0 \left(1 + |kh| \right) \left[\left(\mathcal{M}_h^{-2} + |kh|^{1-p} \right) kh + \frac{2}{|kh|} \right]$$

Chandrasekhar '51, Vandervoort '70, Toomre '77







PFH 2011



PFH 2011



PFH 2011



PFH 2011








The "First Crossing" Mass Function VS GIANT MOLECULAR CLOUDS



The "First Crossing" Mass Function **VS GIANT MOLECULAR CLOUDS**

 $r_{
m sonic} \ll r \ll h$ $S(r) \sim S_0$





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m sonic} \ll r \ll h$ $S(r) \sim S_0$

$$\frac{\mathrm{d}n}{\mathrm{d}M} \propto M^{-\alpha} \, e^{-(M/M_J)^{\beta}}$$







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The "Last Crossing" Mass Function VS PROTOSTELLAR CORES & THE STELLAR IMF



The "Last Crossing" Mass Function VS PROTOSTELLAR CORES & THE STELLAR IMF



"Void" Abundance VS HI "HOLES" IN THE ISM



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Structural Properties of "Clouds" LARSON'S LAWS EMERGE NATURALLY



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Structural Properties of "Clouds" LARSON'S LAWS EMERGE NATURALLY



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Evolve the Fluctuations in Time CONSTRUCT "MERGER/FRAGMENTATION" TREES

$$p(\delta \mid \tau) = \frac{1}{\sqrt{2\pi S \left(1 - \exp\left[-2\tau\right]\right)}} \exp\left[-\frac{\left(\delta - \delta(t=0) \exp\left[-\tau\right]\right)^2}{2 S \left(1 - \exp\left[-2\tau\right]\right)}\right]$$
$$\tau \equiv u_t(k) \, k \, t \sim \frac{t}{t_{\text{cross}}}$$

Evolve the Fluctuations in Time CONSTRUCT "MERGER/FRAGMENTATION" TREES



1. What Maintains the Turbulence?

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Efficient Cooling: $\dot{P}_{\rm diss} \sim \frac{M_{\rm gas} v_{\rm turb}}{t_{\rm crossing}}$

2. Why Doesn't Everything Collapse?

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Efficient Cooling: $\dot{P}_{\rm diss} \sim \frac{M_{\rm gas} v_{\rm turb}}{t_{\rm crossing}}$

2. Why Doesn't Everything Collapse?



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Why Doesn't Everything Collapse? Q: WHY IS STAR FORMATION SO INEFFICIENT?



Stellar Feedback is Key to Galaxy Formation! SO WHAT'S THE PROBLEM?

 Standard (in Galaxy Formation):
 Couple SNe energy as "heating"/thermal energy

FAILS:

$$t_{\rm cool} \sim 4000 \,{\rm yr} \left(\frac{n}{{\rm cm}^{-3}}\right)^{-1}$$

 $t_{\rm dyn} \sim 10^8 \,{\rm yr} \left(\frac{n}{{\rm cm}^{-3}}\right)^{-1/2}$



- Turn off cooling
- Force wind by hand
 ('kick' out of galaxy)





 High-resolution (~1pc), molecular cooling (<100 K), SF only at highest densities (n_H>1000 cm⁻³)



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- "Energy Injection":
 - SNe (II & Ia)
 - Stellar Winds
 - Photoionization (HII Regions)
- *Explicit* Momentum Flux:
 - Radiation Pressure

$$\dot{P}_{\rm rad} \sim \frac{L}{c} \left(1 + \tau_{\rm IR}\right)$$

> SNe

$$\dot{P}_{\rm SNe} \sim \dot{E}_{\rm SNe} \, v_{\rm ejecta}^{-1}$$

Stellar Winds

$$\dot{P}_{\rm W} \sim \dot{M} v_{\rm wind}$$





Energy (dilute gas)

Heat to $C_s > V_{esc}$: unbound

eg: solar wind SN-heated galactic wind



Momentum

(dense gas; energy radiated)

Force induces δV : if ${\sim}V_{esc}$ drive wind

eg: O-star winds molecular gas δV's



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Shock-heated gas acts on cold gas iff $p_{ m hot} \gtrsim \pi G \Sigma_g^2$





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 $p_{\rm hot} \gtrsim \pi G \Sigma_g^2 \rightarrow \dot{E}_{\rm cool} \gg \dot{E}_{\rm SNe} \text{ for } \Sigma_g \gtrsim 0.02 \,\mathrm{g \, cm^{-2}}$





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Hot gas can vent: cannot affect bulk of gas mass

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Colla

$$\dot{P}_* \sim \dot{P}_{\text{diss}}$$

 $\dot{P}_* \sim \text{few} \times \frac{L}{c} \sim \epsilon_* \dot{M}_* c$

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$$\dot{P}_* \sim \dot{P}_{\rm diss}$$

$$\dot{P}_* \sim few \times \frac{L}{c} \sim \epsilon_* \, \dot{M}_* \, c$$

$$\longrightarrow \dot{\Sigma}_* \sim \left(\frac{\sigma}{\epsilon_* c}\right) \, \Sigma_{\rm gas} \Omega \sim 0.02 \, \Sigma_{\rm gas} \Omega$$







Spiral Galaxy M101 Spitzer Space Telescope • Hubble Space NASA / JPL-Caltech / ESA / CXC / STScl









Hopkins, Quataert, & Murray, 2011b















Hopkins, Quataert, & Murray, 2011b



Compare GMC Mass Function INDEPENDENT OF FEEDBACK, ONCE TURBULENCE MAINTAINED





PFH, Quataert, & Murray, 2011b

BUT, GMCs are Short-Lived FEEDBACK "RECYCLES" MASS: STEADY-STATE MASS FUNCTION



SMC 100 pc





PFH, Quataert, & Murray, 2011b

BUT, GMCs are Short-Lived PREVENTS RUNAWAY COLLAPSE



KEEP?



Stellar Feedback gives Self-Regulated Star Formation



Stellar Feedback gives Self-Regulated Star Formation



Stellar Feedback gives Self-Regulated Star Formation



Kennicutt-Schmidt relation emerges naturally



PFH, Quataert, & Murray, 2011a

Kennicutt-Schmidt relation emerges naturally



PFH, Quataert, & Murray, 2011a

Kennicutt-Schmidt relation emerges naturally



PFH, Quataert, & Murray, 2011a

Global Star Formation Rates are INDEPENDENT of High-Density SF Law



Hopkins, Quataert, & Murray 2011 also Saitoh et al. 2008

Global Star Formation Rates are INDEPENDENT of High-Density SF Law



> Set by feedback (i.e. SFR) needed to maintain marginal stability

Hopkins, Quataert, & Murray 2011 also Saitoh et al. 2008



Gas

How Efficient Are Galactic Super-Winds? DOES IT RESOLVE THE GALAXY MASS FUNCTION PROBLEM?

PFH, Quataert, & Murray, 2011c



Future Directions WHAT CAN WE EXPLORE WITH MORE REALISTIC ISM/FEEDBACK PHYSICS?

- Galactic "Super-Winds"
- Star & Globular Cluster Formation
- Mergers & Starbursts: ~1000x "normal" densities (D. Narayanan, T.J. Cox)
- Cosmological:
 - Galaxy disk formation (D. Keres)
 - Dwarf populations: CDM "crisis"? (M. Kuhlen)
- AGN Feedback: Physics & Coupling:
 - Radiation Pressure, Relativistic Jets, Accretion Disk Winds (D. Kasen, J. DeBuhr, N. Roth)







ISM structure derives from supersonic turbulence + gravity:

- Lognormal density PDF: Gaussian random field
- Predict & understand:
 - GMC Mass Function & Structure ("first crossing")
 - Stellar IMF ("last crossing")
 - > (Nearly) scale-free collapse in turbulent field
 - Clustering of Stars
 - General Turbulent Collapse (e.g. "turbulent box" simulations)

Star formation is Feedback-Regulated: independent of small-scale SF 'law'

- Need 'enough' stars to offset dissipation (set by gravity)
- Leads to Kennicutt relation & super-winds
- Different mechanisms dominate different regimes:
 - > High densities: radiation pressure
 - Intermediate: HII heating, stellar wind momentum
 - Low densities: SNe & stellar wind shock-heating
 - > No *one* mechanism works